

# **FQPSK-O: An Improved Performance Constant Envelope Modulation Scheme for OQPSK**

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## **ABSTRACT**

A new constant envelope modulation scheme for OQPSK, called FQPSK-O, is presented. This modulation technique is an extension of the Feher Quadrature Shift Keying (FQPSK) patented technologies, see Ref[1]. This scheme uses cubic spline interpolation to generate very smooth baseband waveforms in order to increase the spectral and power efficiency. Being a constant envelope modulation, FQPSK-O can operate with class C power amplifier without spectrum regrowth. We achieve a more compact spectrum with comparable bit error rate performance. For example, the spectrum of FQPSK-O is 25% narrower than that of GMSK with  $BT_b=0.3$  and FQPSK-1 with hardlimiter [2] at -40 dB attenuation point. For coherent demodulation under AWGN channel, FQPSK-O has almost the same BER performance as FQPSK-1 with hardlimiter. Both of them are better than GMSK with  $BT_b=0.3$  for  $BER < 10^{-4}$ . In Rayleigh fading channel, FQPSK-O outperforms GMSK with  $BT_b=0.3$  by 2 dB. FQPSK-O is an excellent scheme for wireless and satellite communications which require high spectral and power efficiency.

## **KEY WORDS**

Modulation, FQPSK Feher's quadrature phase shift keying, OQPSK, non-linear amplification, and bandwidth efficiency.

## 1. Introduction

Constant envelope modulation techniques such as MSK, GMSK, and digital FM can be non-linearly amplified without spectral regeneration. This is particularly important for portable phones where battery power supply is limited. Modulation techniques can improve the efficiency of wireless system significantly, with impact on cost, size, power and spectral efficiency, data transmission, throughput speed, and capacity. The proper combination of modulation and RF amplification technologies can further improve the power and spectral efficiency of communication system.

OQPSK has been widely used for digital modulation. For example, GMSK with  $BT_b=0.3$  has been adopted by GSM standard. GMSK with coherent demodulator can be viewed as an OQPSK-type of signal [2]. FQPSK is another well-known OQPSK-type modulation with good spectral and power efficiency. In this paper, we compare the performance of FQPSK-O with that of GMSK with  $BT_b=0.3$  and FQPSK-1 in detail. Further information on this subject can be found in [5].

An architecture and algorithm for constant envelope modulation with good spectral and power efficiency, named FQPSK-O, is presented. Being a constant envelope modulation, FQPSK-O can operate with class C power amplifier without spectrum regrowth. A compact spectrum is achieved by applying the cubic spline interpolation to generate OQPSK-type signals.

In section 2, the transmitter architecture is described. The block diagram and phase mapping algorithm are discussed. We compare the phase trellis and I/Q channel baseband waveforms of FQPSK- I and FQPSK-O. The power spectrum of FQPSK-O is obtained by simulation and hardware experiment.

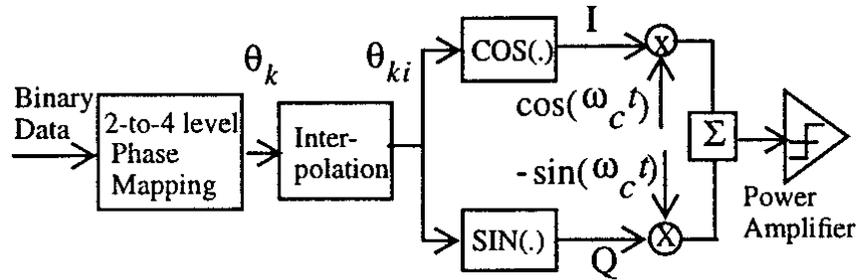
In section 3, the BER performance is obtained by simulation. It shows that FQPSK-O is more power efficient than that of GMSK with  $BT_b=0.3$  for  $BER < 10^{-4}$  in AWGN channel. In Rayleigh fading environment, FQPSK-O outperforms GMSK with  $BT_b=0.3$  by 2 dB.

We conclude in section 4 that the spectral and power efficient FQPSK-O is an excellent scheme for wireless and satellite communications.

## 2. Transmitter

### 2.1 Simulation model

The architecture of the FQPSK-O modulation is shown in Fig. 1. The input binary data bits with duration  $T_b$  are mapped into four possible phase angles. This phase mapping algorithm is the same as that of OQPSK. Therefore, FQPSK-O is compatible with the existing OQPSK coherent demodulators. In each symbol duration, two phase values are generated. This sequence of phase values  $\theta_k$  are interpolated to achieve smooth phase transitions. The number of the interpolated values per symbol is chosen large enough, in order to have an acceptably small aliasing error and thus simplify the low-pass filter design. The sine and the cosine values of the interpolated phase  $\theta_{ki}$  are obtained by table lookup, where  $\theta_{ki}$  is the  $i$ -th interpolated phase value of the  $k$ -th symbol. These are the In-phase and Quadrature (I/Q) baseband signals, which are used to modulate the carrier. By summing these two modulated signals, we have a constant envelope signal which can be non-linearly amplified without spectral regeneration.



**Fig.1** Block diagram of the transmitter of FQPSK-O system.

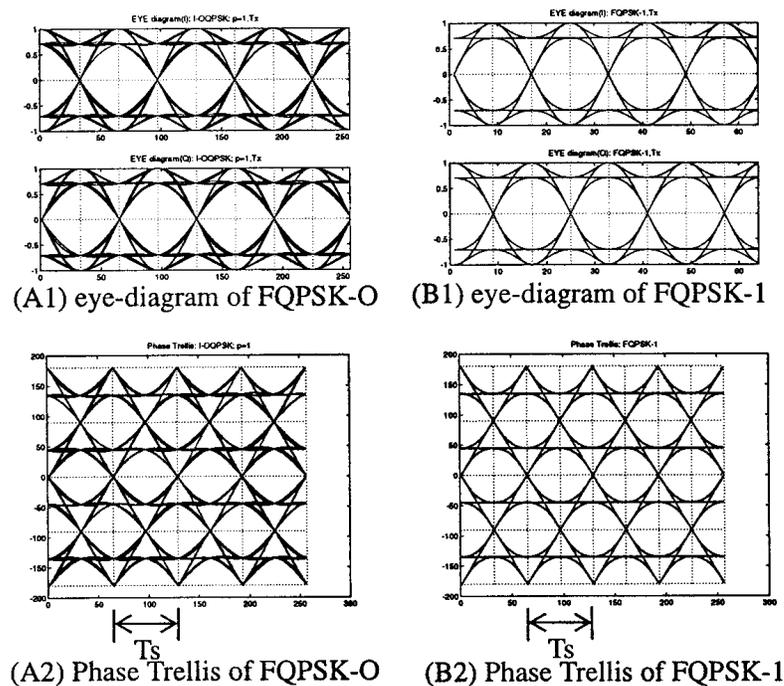
In this paper, we use cubic spline interpolation [3]. Other interpolation methods such as linear interpolation, cubic interpolation, cubic smoothing spline, and spline with tension [4] have also been considered in [5].

In the actual implementation of the transmitter,  $I_{ki} = \text{COS}(\theta_{ki})$  and  $Q_{ki} = \text{sin}(\theta_{ki})$  are converted to analog signals and then fed to low pass filters to remove higher frequency components. The analog I/Q baseband signals are modulated with the carrier, added together and amplified. Due to its constant envelope, FQPSK-O can be amplified with fully non-linear (saturated, C-class or hard-limited) power amplifier without spectral regrowth. Since we are using cubic spline interpolation, the phase is defined by a third-order polynomial of time within each symbol duration. By taking the derivative of the phase with respect to time, we obtain the frequency as a second-order polynomial of time. Hence, we could implement FQPSK-O as a frequency modulation using a voltage-controlled oscillator.

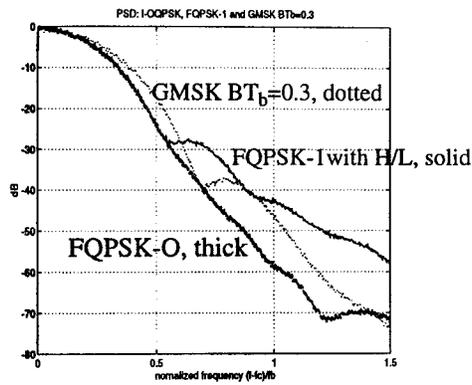
In the simulation, we use baseband equivalent model. The I/Q baseband signals are passed through the channel model. The receiver BPF is replaced by its equivalent LPF.

The I/Q channel eye diagram and phase trellis are plotted in Fig.2. The corresponding diagram for FQPSK-1 with hard-limiter [2] are plotted in the right column of Fig.2 for comparison. Note that the waveforms of FQPSK-O have more variations than that of FQPSK-1. As a result, the side-lobe of the FQPSK-O spectrum is narrower than that of FQPSK-1 and GMSK with  $BT_b=0.3$  (Fig.3). The PSD of FQPSK-O has the same main-lobe as that of FQPSK-1 with hardlimiter till -27 dB attenuation. After -27 dB point, the PSD of FQPSK-O is better than that of FQPSK-1 with hardlimiter where it starts to regrow. Moreover, the PSD of FQPSK-O is better than that of GMSK with  $BT_b=0.3$  till -70 dB attenuation. For example, FQPSK-O is 25% better than GMSK with  $BT_b=0.3$  and FQPSK-1 with hardlimiter at -40 dB attenuation point.

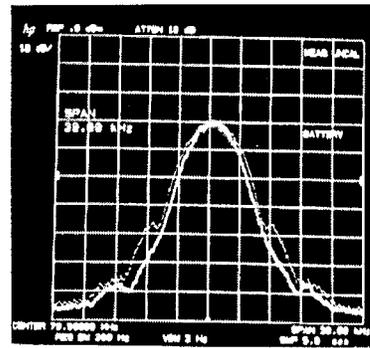
The ratio of out-of-band power to total power are plotted in Fig.4. The horizontal axis of Fig.4 is the channel spacing normalized by bit rate. Based on the definition of the 99% in-band-power, FQPSK-O has a spectral efficiency of 1.3 b/s/Hz, while GMSK with  $BT_b=0.3$  has a spectral efficiency of 1.1 b/s/Hz.



**Fig.2** I/Q channel eye diagram and phase trellis: (A) FQPSK-O (B) FQPSK-1 with hardlimiter

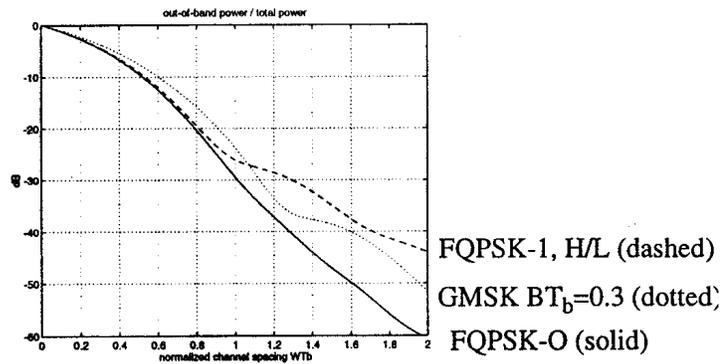


(A) simulation results



(B) experiment results:  
 upper trace: GSMK  $BT_b=0.3$   
 lower trace: FQPSK-O  
 spectrum analyzer:  
 vertical: 10 dB/div  
 horizontal: 3K Hz/div  
 (span=30K Hz)  
 sweep time= 5 sec  
 center freq. ( $f_c$ ) = 70M Hz  
 input data rate: 7.27 K b/s

**Fig.3** PSD of FQPSK-0, FQPSK- I with hardlimiter and GSMK  $BT_b=0.3$ .

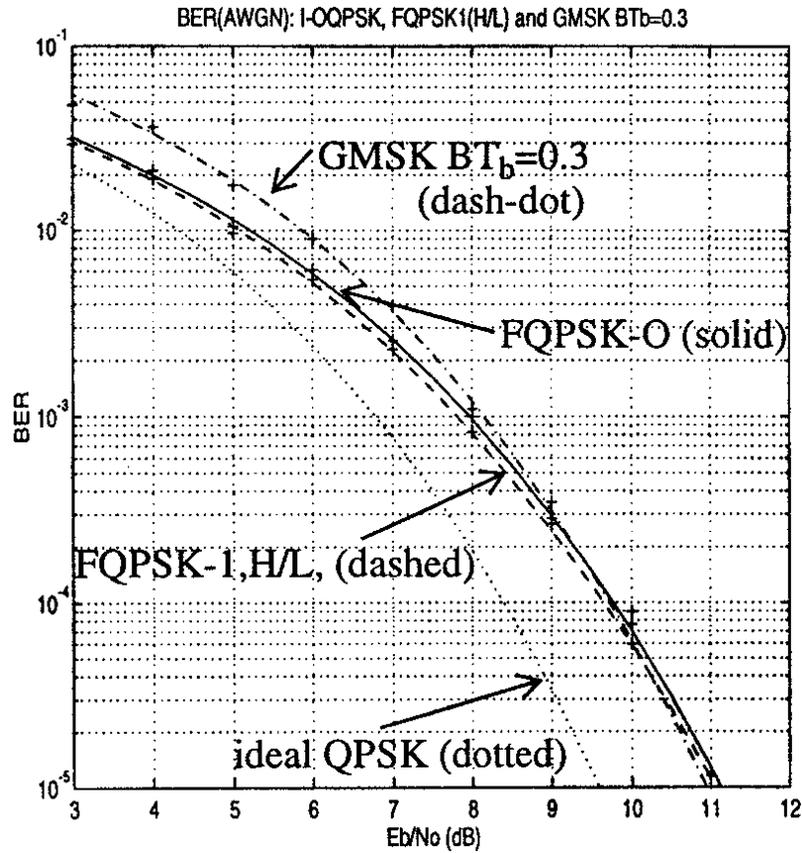


**Fig.4** Out-of-B and Power vs. Normalized Channel Spacing plot.

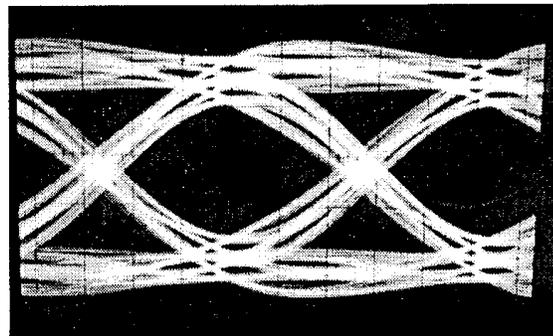
### 3. BER performance

The BER performance of the coherent demodulation of FQPSK-O, FQPSK-1 and GSMK with  $BT_b=0.3$  in AWGN channel are obtained by computer simulations as shown in Fig.5. The receiver BPF for FQPSK-O is a Butterworth 4th order filter with  $B_iT_b=0.55$ . For GSMK with  $BT_b=0.3$  and FQPSK-1, a Butterworth 4th order BPF with  $B_iT_b=0.6$  is employed. Fig. 6 shows the eye diagram for the receiver.

Note that the eye openings are asymmetrical due to the non-constant group delay of the receiver BPR FQPSK-O is about 0.2 dB worse than FQPSK-1 with hardlimiter. Both FQPSK-O and FQPSK-1 outperform GSMK with  $BT_b=0.3$  for  $E_b/N_o < 10^{-4}$ . Similar results of comparing FQPSK-1 and GSMK are given in [6].

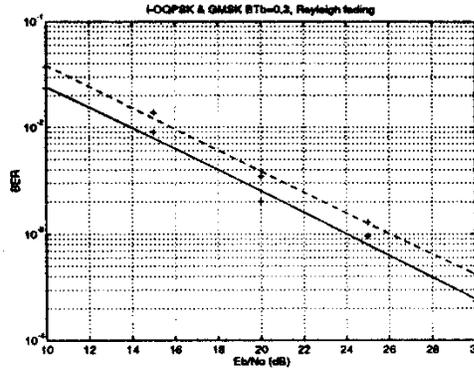


**Fig.5** BER performance of coherent demodulation of FQPSK-O, FQPSK-1 (hardlimiter), GSMK with  $BT_b=0.3$  and ideal QPSK with AWGN.



**Fig.6** Eye diagram of the coherently demodulated FQPSK-O signals. Only in-phase channel is shown. The bit rate is 7.27k b/s. The receiver LPF is a Butterworth 4th order LPF with cut-off frequency at 2.0k Hz, which corresponds to a normalized IF bandwidth of  $B_i T_b=0.55$ .

The BER performance of the coherent detection of FQPSK-O in slow Rayleigh fading channel is depicted in Fig.7. Here, we assume perfect Carrier Recovery (CR) and Symbol Time Recovery (STR). To obtain this result, we use the same set of receiver BPF as in the AWGN case. The normalized Doppler frequency is  $f_D T_b = 1.65 \times 10^{-3}$ , that corresponds to a 40 Hz Doppler and a data rate of 24.3K b/s. A Butterworth 4th order receiver BPF with  $B/T_b = 0.55$  is employed for FQPSK-O. Ideal Gaussian BPF with  $B/T_b = 0.6$  is used for GMSK with  $B/T_b = 0.3$ . Comparing with coherent detection of GMSK with  $B/T_b = 0.3$ , FQPSK-O is 2 dB better under the same BER requirements.



**Fig.7** BER performance of FQPSK-O and GMSK with  $B/T_b = 0.3$  as a function of  $E_b/N_0$  in Rayleigh fading channel. FQPSK-O outperforms GMSK by 2 dB.

#### 4. Conclusion

A new modulation scheme for OQPSK using cubic spline interpolation is presented. It increases the spectral and power efficiency. Being a constant envelope modulation, FQPSK-O can be operated with class C power amplifier without spectrum regrowth. FQPSK-O has a narrower spectrum than that of GMSK with  $B/T_b = 0.3$  till 70 dB attenuation. Especially, it has 20% - 30% better spectral efficiency than that of GMSK with  $B/T_b = 0.3$  from 40 dB to 70 dB attenuation. FQPSK-O is more power efficient than that of GMSK  $B/T_b = 0.3$  for  $BER < 10^{-4}$  in AWGN channel. In Rayleigh fading, FQPSK-O outperforms GMSK  $B/T_b = 0.3$  by 2 dB. Thus, FQPSK-O is an excellent scheme for wireless and satellite communications which require high spectral and power efficiency.

#### 5. Acknowledgments

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## 6. References

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