

# ETF Arbitrage, Non-Fundamental Demand, and Return Predictability\*

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**Abstract.** Non-fundamental demand shocks have significant effects on asset prices, but observing these shocks is challenging. We use the exchange traded fund (ETF) primary market to study non-fundamental demand. Unique to the ETF market, specialized arbitrageurs called authorized participants correct violations of the law of one price between an ETF and its underlying assets by creating or redeeming ETF shares. We show theoretically and empirically that creation and redemption activities (ETF flows) provide signals of non-fundamental demand shocks. A portfolio which is short high-flow ETFs and long low-flow ETFs earns excess returns of 1.1% to 2.0% per month, consistent with non-fundamental demand distorting asset prices away from fundamental values. Moreover, we show non-fundamental demand imposes non-trivial costs on investors, leading to underperformance.

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## 1. Introduction

Non-fundamental demand shocks cause asset prices to deviate from their fundamental values. In turn, this can lead to financial market externalities that cause distortions in real investment and output.<sup>1</sup> Despite the importance of non-fundamental demand shocks for financial markets and the real economy, measuring them remains a challenge. Identifying non-fundamental demand shocks from stock price changes is difficult because fundamentals values are unobservable. Similarly, identifying non-fundamental demand from trading volume is difficult because volume does not reveal the underlying motivations for trading. Even mutual fund flows are confounded by information about fund manager skill, making it difficult to disentangle non-fundamental demand from demand for specific fund managers.<sup>2</sup>

In this paper, we show theoretically and empirically that exchange traded funds (ETFs) offer a unique setting to identify and study non-fundamental demand. We develop a model of the ETF market to demonstrate that ETF flows are symptomatic of shocks that dislocate prices from fundamental values. The intuition is simple: while fundamental value is inherently unobservable, ETFs and their underlying assets share the same fundamental value. Thus, violations of the law of one price between the two signal that at least one of them was affected by non-fundamental demand (e.g., sentiment, noise, etc.). Unique to the ETF market, specialized arbitrageurs called authorized participants correct violations of the law of one price by creating or redeeming ETF shares. Because these creations or redemptions by authorized participants (i.e., ETF flows) are publicly observable, they provide a novel signal of the occurrence of non-fundamental demand.<sup>3</sup>

<sup>1</sup> For example, several papers on mutual fund fire sales argue that non-fundamental demand shocks cause fund managers to liquidate holdings. This causes other assets to decline in value, thereby decreasing the value of firms and causing reductions in aggregate investment and output (e.g., Lorenzoni, 2008; Shleifer and Vishny, 2011).

<sup>2</sup> Mutual fund flows have been shown to contain information about investor demands and/or sentiment (e.g., Sirri and Tufano, 1998; Ippolito, 1992; Cooper, Gulen and Rau, 2005; Lou, 2012; Kamstra et al., 2017). Theory suggests that mutual fund flows are also contaminated by information about fund manager skill (e.g., Berk and Green, 2004). Warther (1995) and Ben-Rephael, Kandel and Wohl (2012) examine flows aggregated across mutual funds to measure aggregate investor sentiment allowing them to avoid the confounding influence of fund manager skill.

<sup>3</sup> Importantly, ETF flows are *primary* market trades that are distinct from the secondary market trades of ETF investors. While ETF investors may trade for fundamental reasons,

We confirm the model's predictions and show empirically that ETFs provide valuable conditioning information to identify fundamental mispricing. That is, ETF flows predict future asset returns in both an ETF's shares and its underlying assets, consistent with non-fundamental demand generating mispricings that subsequently reverse. Given that most ETFs are passively managed, are traded by a rich cross section of investors and encompass nearly every asset class, our findings show ETF flows provide arguably the cleanest and most extensive measure of non-fundamental demand shocks to date. Moreover, our analysis allows us to explore the implications of non-fundamental demand; we find it imposes economically significant costs on investors. For example, in State Street's S&P 500 ETF (SPY), the largest ETF in the world, investors bear additional indirect costs that are an order of magnitude larger than the ETF's explicit management fee.

We start by developing a parsimonious model of the ETF market based on its prominent features: (i) both ETF shares and ETF underlying assets are traded in secondary markets, (ii) unlike open-ended mutual funds, the prices of ETF shares may differ from the prices of the underlying assets, (iii) unlike closed-end funds, authorized participants restore relative price efficiency via primary market activities, and (iv) unlike most open-end and closed-end funds that are actively managed, ETFs are passively managed.<sup>4</sup> Authorized participants create new ETF shares by delivering the underlying assets if the ETF shares are trading at a premium or, conversely, authorized participants redeem ETF shares for the underlying assets if the ETF shares are trading at a discount. We solve for authorized participants' equilibrium arbitrage activity (i.e., ETF flows), the equilibrium ETF price, and the equilibrium underlying assets' prices. We show that ETF flows are signals of unobservable non-fundamental demand shocks. Put differently, ETF flows can identify unobservable fundamental mispricing.

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we focus only on primary market trades that occur because of violations of the law of one price.

<sup>4</sup> Closed-end funds do not have authorized participants who enforce the law of one price between the fund shares and the underlying assets. As a result, the funds can trade at a premium or, more often, at a significant discount (relative to the underlying). Previous studies have examined these large and persistent mispricings and offer a wide range of explanations: managerial skill and fees (Berk and Stanton, 2007), liquidity (Cherkes, Sagi and Stanton, 2008), costly arbitrage capital (Pontiff, 1996), and investor sentiment (Lee, Shleifer and Thaler, 1991; Baker and Wurgler, 2006).

Figure 1 illustrates the mechanism. At  $t=0$ , both the ETF and the underlying assets share the same price. At  $t=1$ , latent non-fundamental demand shocks arrive and push the price of the ETF above the underlying net asset value (NAV). These demand shocks could differentially affect the ETF and the underlying assets, either because the demand shock that hits the ETF is larger than the shock to the underlying assets or because the ETF is relatively more sensitive to demand shocks. This leads to an ETF premium (i.e., a relative mispricing). At  $t=2$ , authorized participants buy shares in the underlying assets and sell shares in the ETF to correct the relative mispricing. They close their trades by creating new shares in the ETF, generating observable ETF flows that reveal the non-fundamental demand shocks. Importantly, while arbitrageurs trade to correct relative mispricing, their trades do not correct fundamental mispricing. Thus, in the long term, the prices of both the ETF and the underlying assets exhibit return predictability as the fundamental mispricing corrects.

While the model succinctly shows that ETF flows signal non-fundamental demand, the result is not driven by the setup or assumptions. Trading by authorized participants *only* occurs if there is a profitable arbitrage trade, and this must indicate that there was excess demand for either the ETF shares or the underlying assets. Since the ETF shares are a claim to the underlying assets, excess demand for either the shares or the underlying assets *must* be due to a non-fundamental force. Of course, it is possible that the non-fundamental force is correlated with fundamental demand, for example, over- or under-reaction to news about future cash flows or discount rates. In this case, what matters is the size of the fundamental shock relative to the non-fundamental component. To use an analogy, ETF flows are akin to observing ice in the ocean; while they are observable, the extent to which they signal large or small fundamental mispricing beneath the surface is unclear. On the one hand, the non-fundamental component signaled by ETF flows may be (i) highly correlated with a fundamental demand shock and (ii) relatively small as compared to the fundamental demand shock. In such a case, return reversals will likely be small, short-lived and hard to detect.<sup>5</sup> That is, there is not much beneath the

<sup>5</sup> For example, Marshall, Nguyen and Visaltanachoti (2013), Madhavan and Sobczyk (2016), and Ben-David, Franzoni and Moussawi (2018) provide evidence consistent with ETF flows' speeding price discovery, particularly when the ETF is more liquid than the un-

surface. On the other hand, the non-fundamental component signaled by ETF flows may be (i) not strongly related to fundamentals and (ii) economically significant. In this case, return predictability is likely to be large. That is, ETF flows are the tip of the iceberg. Ultimately, it is an empirical question whether ETF flows signal large price distortions. We find that they do.

We test the model's predictions using a sample of ETFs over the period 2007 to 2016. We find strong evidence that ETF flows predict future asset returns, consistent with ETF flows' identifying non-fundamental demand. We start our empirical analysis with univariate portfolio sorts examining ETF flows. Each month, we form long-short portfolios based on the prior month's ETF flows; our long-short portfolio buys ETFs with the smallest flows and sells short ETFs with the largest flows. Consistent with our model, we find strong evidence that ETF flows contain information about future asset returns. At a one-month horizon, our long-short portfolio earns returns of 1.1% to 2.0% per month. Moreover, return predictability remains at the three- and six-month horizons indicating that ETF flows signal non-fundamental demand shocks that lead to fundamental mispricing that corrects over time. Because univariate sorts do not control for fund- and time-level heterogeneity, we next turn to a multivariate regression approach. We again find that ETF flows contain information about future asset returns in the cross-section. ETFs in the top decile of flows underperform ETFs in the bottom decile by a statistically significant 1.8% over the next month. This result holds at three- and six-month horizons and remains statistically and economically significant when we examine risk-adjusted returns. Consistent with our model's predictions, we also find that return predictability is strongest in leveraged ETFs and high activity ETFs (defined as those with the most active primary markets), which are characterized by volatile flows. Moreover, the results are not driven by extreme returns in a few sample months. Trading strategies produce annualized Sharpe ratios of 0.60 and 0.99 at the one- and six-month horizons.

Our results document a strong negative relation between ETF flows and subsequent returns. This suggests that non-fundamental demand imposes non-trivial costs on investors. To examine the implications of

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derlying assets. If the non-fundamental shocks signaled by ETF flows are highly correlated with fundamental price discovery, then measurable return predictability is unlikely.

our results for ETF investor profitability, we consider two performance measures; the internal rate of return (IRR) and the share-growth-adjusted return (SGAR). The IRR measures the returns of a representative investor that holds all shares in an ETF and is responsible for all of the ETF's inflows and outflows. The SGAR has an asset allocation interpretation: it considers an investor who rebalances monthly across a risk-free asset and the ETF based on the last month's flows. Both measures speak to the relation between flows and returns, but they differ in important ways. The IRR is agnostic to timing, accounting for the relation between flows and returns at all horizons. This flexibility comes at a cost; the measure cannot distinguish between whether flows lead returns or returns lead flows (Hayley, 2014). The SGAR is intentionally less flexible; by construction, it only examines the relation between last month's flows and the current month's returns. Both measures provide the same conclusion: non-fundamental demand distorts prices and imposes non-trivial costs on ETF investors, leading to underperformance.

We contribute to the literature on the information in investor flows. First, our model is simple and it provides clear intuition for the ETF market. In the same spirit that Berk and Green (2004) shows that mutual fund flows reflect demand for specific managers, our model shows that ETF flows signal non-fundamental demand. As such, we provide a simple workhorse model that may be built upon and utilized in future ETF studies. Second, as noted in Daniel, Hirshleifer, and Subrahmanyam (2001), "... expected returns also depend on current mispricing, so returns can be predicted better by conditioning on proxies for misvaluation." Our paper does this – we provide a novel measure of misvaluation. Many papers find that primary and secondary market flows contain information about investor demands. For example, several papers find that flows into, and out of, mutual funds and hedge funds contain information about future asset returns (Sirri and Tufano, 1998; Ippolito, 1992; Cooper, Gulen and Rau, 2005; Frazzini and Lamont, 2008; Ben-Rephael, Kandel and Wohl, 2012; Lou, 2012; Ben-David, Franzoni and Moussawi, 2012).<sup>6</sup> Our results are related to, but distinct from, these existing findings for three reasons. First, our model

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<sup>6</sup> There is also a large literature that documents a relation between primary market issuances (and related corporate events) and future stocks returns (e.g., Loughran and Ritter, 1995; Loughran and Vijh, 1997; Baker and Wurgler, 2000; Daniel and Titman,

shows that authorized participant trading indicates the occurrence of non-fundamental demand. This is in contrast to other measures of investor flows, like mutual fund flows, which could reflect learning about fund manager skill and thus do not necessarily reflect non-fundamental demand. Second, the signal of non-fundamental demand does not originate from one class of investor; ETFs are used by a broad cross-section of market participants that includes retail traders, large institutions, and hedge funds. Third, we empirically demonstrate that the information in ETF flows is distinct from the information in mutual fund flows: our results are robust to controlling for aggregate mutual fund flows (Ben-Rephael, Kandel and Wohl, 2012) and we do not find return predictability in passively managed index mutual fund flows.<sup>7</sup> Thus, while a number of papers have used mutual fund flows to measure deviations from fundamental values in asset prices, our paper shows that ETF flows provide a powerful and clean measure for use in future studies.

We also provide novel evidence that ETF investors systematically underperform due to non-fundamental demand and display poor timing. Several papers show that investors in other asset classes underperform because of timing effects.<sup>8</sup> In our setting, ETF investors are simply moving into or out of a passively managed basket of securities. As these flows originate from a diverse group of investors, it is perhaps surprising that these ETF investors collectively mistime their flows. However, these results are reconcilable with our model; ETF flows signal non-fundamental demand shocks that predictably reverse, regardless of the source. Thus, ETF flows aggregate non-fundamental demand shocks from different types of investors.

Our paper adds to the growing literature on the relation between ETFs and other market outcomes.<sup>9</sup> As non-fundamental demand

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2006; Ikenberry, Lakonishok and Vermaelen, 1995; Fama and French, 2008; Pontiff and Woodgate, 2008).

<sup>7</sup> See Tables IA7, IA14, IA22, and IA23 of the Internet Appendix.

<sup>8</sup> Sapp and Tiwari (2004), Friesen and Sapp (2007) and Hsu, Myers and Whitby (2016) show that mutual fund investors chase past returns, leading to negative market-timing and Dichev (2007) finds that investors in equities systematically underperform once distributions and contributions are accounted for.

<sup>9</sup> A number of papers study the direct effects of ETF flows on assets. Baltussen, van Bakkum and Da (2019) and Da and Shive (2018) show that ETFs induce comovement between underlying assets, and Ben-David, Franzoni and Moussawi (2018) and Krause, Ehsani and Lien (2014) document volatility transmission from ETFs to the funds' underlying assets. For more related work, see Bessembinder (2015), Israeli, Lee and Sridharan

shocks can cause both relative and absolute mispricing, our findings complement the results in Ben-David, Franzoni and Moussawi (2018). Ben-David, Franzoni and Moussawi (2018) shows that arbitrageur trades, which are acting to restore relative price efficiency, transmit volatility to the underlying assets via price pressure. They also show that arbitrage activity itself is related to underlying stock prices, which generates return predictability. However, they examine price pressure from arbitrage activity which subsequently reverses at short horizons. In contrast, we show that the need to restore relative price efficiency *in the first place* signals there was a non-fundamental demand shock that generated an absolute mispricing. Empirically, these mispricings are distinct from those studied in Ben-David, Franzoni and Moussawi (2018) and subsequently reverse over horizons of one to six months.<sup>10</sup> Overall, our model provides a microfoundation for using ETF flows as signals of non-fundamental demand shocks and our empirical findings confirm the model’s predictions.

## 2. Model of ETF Trade

In this section, we provide a succinct model which shows that ETF flows must imply a non-fundamental distortion occurred and that ETF flows can signal a fundamental mispricing. Importantly, while the model is built from several assumptions which allow for richer empirical predictions, our insights are not driven by these assumptions. To show this, we begin with a simple thought experiment before developing the model. Consider two traded securities that share the same fundamental value with prices  $A$  and  $B$ , respectively. The law of one price says that  $A$  should equal  $B$ . If  $A \neq B$ , there is a relative mispricing, and  $A - B$  reflects the excess demand for  $A$ . By taking the difference between  $A$  and  $B$ , their shared fundamental value cancels out and the residual must reflect mispricing from non-fundamental excess demand.<sup>11</sup> Thus, trades that exploit the mispricing (i.e., arbitrage trades) imply the re-

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(2017), Jiang and Yan (2020), Staer (2016), Agarwal et al. (2019), Dannhauser (2017), Dannhauser and Hoseinzade (2017), Glosten, Nallareddy and Zou (Forthcoming), Pan and Zeng (2019), Staer and Sottile (2018), and Dannhauser and Pontiff (2019).

<sup>10</sup> See Internet Appendix Section 8 for a detailed discussion.

<sup>11</sup> Note that mispricing between  $A$  and  $B$  could be correlated with fundamental demand. In Section 7 of the Internet Appendix, we provide additional discussion and we address several misconceptions regarding the ETF market mechanism.

alization of this non-fundamental excess demand. As the model will show, ETF flows always signal a non-fundamental force.

Consider a four period model  $t \in \{0, 1, 2, \textit{long term}\}$  in which a passively managed ETF provides exposure to a benchmark index (e.g., the S&P 500). In period  $t = 0$ , initial prices for the ETF shares and the ETF underlying assets are set. At  $t = 1$ , both fundamental news and non-fundamental distortions are realized, potentially giving rise to a relative mispricing.<sup>12</sup> At  $t = 2$ , arbitrageurs called authorized participants trade against the mispricing and equilibrium prices for the shares and the underlying assets are determined. The equilibrium prices are not necessarily equal to fundamental value. At  $t = \textit{long term}$ , prices return to fundamental value. We elaborate below.

In each period  $t$ , there is a  $q_t$ -length measure of ETF shares and the market value of each share is denoted  $p_t$ . The underlying assets backing the ETF shares mirror the benchmark index. Each unit of the ETF's underlying assets has an unobservable fundamental value  $\Omega_t$  and a tradable value  $\pi_t$  (i.e., net asset value or NAV). For simplicity, the number of units of the underlying asset held by the ETF are also  $q_t$  so that the NAV per ETF share is  $\pi_t$ . In each period, the ETF premium is the difference in  $p_t$  and  $\pi_t$ ,

$$\psi_t \equiv p_t - \pi_t. \quad (1)$$

A non-zero value of  $\psi_t$  represents a violation of the law of one price. A non-zero value of  $\psi_t$  is a *true-arbitrage* opportunity as there is a long-short trade to exploit the mispricing.

Define the *ETF fundamental mispricing* as the difference between the ETF share price and its unobservable fundamental value,

$$\varphi_t = p_t - \Omega_t, \quad (2)$$

and define the *NAV fundamental mispricing* as the difference between the NAV per share and its unobservable fundamental value,

$$\alpha_t = \pi_t - \Omega_t. \quad (3)$$

Non-zero values of  $\varphi_t$  and  $\alpha_t$  reflect fundamental mispricing, sometimes referred to as a *risky-arbitrage* opportunity. However, the mispricing is not observable because  $\Omega_t$  is latent. Even if one has a signal regarding

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<sup>12</sup> Our use of the term “non-fundamental” includes beliefs that are uncorrelated with fundamental news and also over- and under-reaction to fundamental news.

the values of  $\varphi_t$  and  $\alpha_t$ , there is not a risk-free trading strategy that can capture the mispricing.

In addition to the ETF shares and the underlying assets trading in a secondary market, there also exists a primary market for the ETF shares. The primary market is constituted by  $N \geq 1$  authorized participants and the ETF sponsor (e.g., BlackRock). In response to a relative mispricing ( $\psi_t \neq 0$ ), each of the  $N$  authorized participants may deliver the underlying assets in exchange for *new* ETF shares or may deliver *existing* ETF shares in exchange for the underlying assets.<sup>13</sup> We denote each authorized participant  $i$ 's arbitrage demand (share creations or share redemptions) at time  $t$  as  $\delta_{t,i}$  and the aggregate demand of all authorized participants at time  $t$  as  $\Delta_t = \sum_{i=1}^N \delta_{t,i}$ .  $\Delta_t$  may be positive in value (ETF shares are created in net) or  $\Delta_t$  may be negative in value (ETF shares are redeemed in net). Thus,  $\Delta_t$  measures investor flows in and out of the underlying assets through the ETF; we refer to  $\Delta_t$  as the ETF flow hereafter. Because the ETF flow only occurs at  $t = 1$ , we drop the subscript  $t$ .

The market price for ETF shares is determined by the intersection of ETF share supply and aggregate ETF investor demand. Investors' collective demand is downward-sloped,

$$p_t = \Omega_t + \beta - \eta q_t + \epsilon_t^{etf}, \quad (4)$$

in which  $\Omega_t$  is the latent fundamental value,  $\beta \geq 0$  is a constant so that the initial shares outstanding are strictly positive and  $\eta \geq 0$  proxies for investors' sensitivity to the measure of shares. A downward-sloped demand curve is micro-founded on investor risk aversion and lower values of  $\eta$  imply less price impact from ETF flows. The variable  $\epsilon_t^{etf}$  is a non-fundamental component to ETF investor demand drawn from a mean zero distribution with variance  $\sigma_e^2$ . We are agnostic to the source of the non-fundamental demand component; it could be due to noise/liquidity trading (Black, 1986; De Long et al., 1990) or investor sentiment (Lee, Shleifer and Thaler, 1991; Baker and Wurgler, 2006; Baker and Wurgler, 2007; Frazzini and Lamont, 2008). Or, the non-fundamental demand component could be due to characteristics of trading in the ETF

<sup>13</sup> Without loss of generality, for derivatives based ETFs (e.g., leveraged ETFs), the authorized participants may deliver cash in the amount of NAV for an ETF share and vice versa.

that differ from trading in the underlying assets. For example, trading costs often render the ETF cheaper than buying the underlying assets individually. Alternatively, the non-fundamental demand component could be over- or under-reaction to fundamental news. Importantly, the non-fundamental component is *any* tension that distorts the ETF price away from fundamentals. From here forward, we refer to the non-fundamental component as a non-fundamental demand shock without loss of generality.

The NAV is given by,

$$\pi_t = \Omega_t + \epsilon_t^{nav} + \lambda\Delta, \quad (5)$$

in which  $\Omega_t$  is the latent fundamental value and  $\epsilon_t^{nav}$  is an aggregate non-fundamental shock to the underlying asset demand drawn from a mean zero distribution with variance  $\sigma_n^2$ . Similar to  $\epsilon_t^{etf}$ ,  $\epsilon_t^{nav}$  is any non-fundamental tension that distorts the NAV. Additionally, the trading activity of authorized participants may create price pressure on the underlying asset via  $\lambda \geq 0$ . For example, if the price of the underlying assets are determined by a market maker that does not observe the ETF flow, she may interpret trades as signals of the assets' fundamental value as in Kyle (1985). Alternatively,  $\lambda$  may be determined by investor risk aversion as a positive value of  $\lambda$  implies that investor demand for the underlying assets is also downward-sloped.

The ETF shares' and ETF underlying assets' shared latent fundamental value  $\Omega_t$  is given by,

$$\Omega_t = \Omega_{t-1} + \omega_t, \quad (6)$$

in which  $\omega_t$  is fundamental news (i.e., a fundamental shock) distributed according to a zero-mean distribution.

Importantly, we allow non-fundamental demand shocks to hit both the ETF shares and the underlying assets. For example, our model can handle the possibility that the ETF shares attract sentiment trades and also that the underlying assets are illiquid. In this example, there are non-fundamental forces at work in *both* the ETF shares and the underlying assets; the ETF share prices may be pushed around by sentiment trades while the underlying asset prices are stale. As we show shortly, equilibrium ETF flows are linear in the difference of these two non-fundamental demand shocks. In other words, what is important is the net non-fundamental demand between the ETF shares and the

underlying assets. We denote the correlation between  $\epsilon_t^{etf}$  and  $\epsilon_t^{nav}$  as  $\rho = \frac{\text{Cov}(\epsilon_t^{etf}, \epsilon_t^{nav})}{\sigma_e \sigma_n}$ . Furthermore,  $\epsilon_0^{etf} = 0$  and  $\epsilon_0^{nav} = 0$  and, as such, we drop the subscript  $t$  hereafter. This implies that  $\pi_0 = \Omega_0$ . The initial measure of the ETF's shares  $q_0$  is set so that an ETF premium does not initially exist and the ETF is fairly priced with respect to fundamental value.  $q_0 \equiv \frac{\beta}{\eta}$  solves,

$$\pi_0 = \beta + \Omega_0 - \eta q_0. \quad (7)$$

Within period  $t = 1$ : (i) demand shocks  $\epsilon^{etf}$ ,  $\epsilon^{nav}$ , and  $\omega_t$  are realized, and (ii) investor demands shift for the ETF shares and the underlying assets, giving rise to an interim ETF premium  $\psi_1$ . At  $t = 2$ : (i) authorized participants buy the less expensive asset and sell the more expensive asset, generating price pressure on both the ETF shares and the underlying assets, (ii) authorized participants create or redeem shares to complete the arbitrage trade, and (iii) the equilibrium prices for the ETF shares and the ETF underlying assets are established. In practice, the time between  $t = 1$  and  $t = 2$  may take place over an instant as arbitrageurs quickly restore relative price efficiency.

To provide the most natural and intuitive explanation of our model, we focus on the special case in which  $\rho = 1$ ,  $\sigma_e \neq \sigma_n$  and in the limit  $N \rightarrow \infty$ . Assuming  $\rho = 1$  implies that the non-fundamental demand shocks to the ETF shares and to the underlying assets are perfectly correlated, and assuming  $\sigma_e \neq \sigma_n$  implies that a non-fundamental demand shock gives rise to a relative mispricing. Considering the limiting case in which  $N \rightarrow \infty$  focuses on perfect competition among authorized participants. A general solution to the model is located in the Appendix.

**Remark 1.** The ETF primary market mechanism's ability to restore relative price efficiency requires,  $\eta > 0$ ,  $\lambda > 0$ , or both.

ETF design, both in our model and in practice, is predicated on the requirement that relative price efficiency is restored by affecting the supply of ETF shares. Remark 1 highlights that affecting the supply of ETF shares has a price effect if, and only if, either the demand for the ETF shares is downward sloping, the demand for the underlying assets is downward sloping, or both.

After the demand shocks are realized, each authorized participant  $i$  chooses a length  $\delta_i \in \mathfrak{R}$  of shares to create or redeem in the ETF to exploit the true-arbitrage opportunity. Each authorized participant solves the following optimization,

$$\max_{\delta \in \mathfrak{R}} \delta_i (p_2(\delta_i | \delta_{-i}) - \pi_2(\delta_i | \delta_{-i})), \quad (8)$$

in which  $\delta_{-i}$  is the creation/redemption activity of the other authorized participants.

**Lemma 1.** *The aggregate ETF flow is,*

$$\lim_{N \rightarrow \infty} \Delta^* = \frac{\epsilon^{etf} - \epsilon^{nav}}{\lambda + \eta}. \quad (9)$$

According to Lemma 1, the equilibrium ETF flow does not contain the fundamental shock  $\omega_1$  and is linear in the difference of the two non-fundamental demand shocks.<sup>14</sup> As such, there is a natural economic interpretation to the ETF flow outlined in Equation 9: ETF flows occur when there is net excess demand in either the ETF shares or the ETF underlying assets. When the net excess demand favors the ETF shares, there is a positive flow (i.e., share creations). When the net excess demand favors the ETF underlying assets, there is a negative flow (i.e., share redemptions).

**Remark 2.** ETF flows are symptomatic of non-fundamental demand distortions.

Equation 9 and Remark 2 motivate our empirical analyses by showing that ETF flows are sufficient to identify that at least one non-fundamental demand shock occurred (either in the ETF share demand, the ETF underlying asset demand, or in both). A non-fundamental shock could be attributed to many sources: under- or over-reaction to fundamental news, market frictions, liquidity shocks, and investor sentiment shocks.<sup>15</sup> Notably, while the demand for the ETF shares and the demand for the underlying assets both contain the fundamental component, the fundamental component does not directly show up in

<sup>14</sup> Proofs of Lemma 1, Lemma 2 and Proposition 1 are in the Appendix.

<sup>15</sup> See Hirshleifer (2001) and Barberis and Thaler (2003) for surveys of the behavioral finance literature.

the relative mispricing.<sup>16</sup> As a consequence, ETF flows provide a clean signal that a non-fundamental demand shock occurred.

**Lemma 2.** *The variance of the ETF flow is,*

$$\lim_{N \rightarrow \infty} \text{Var}(\Delta^*) = \frac{\sigma_e^2 + \sigma_n^2 - 2\rho\sigma_e\sigma_n}{(\lambda + \eta)^2}, \quad (10)$$

and  $\text{Var}(\Delta^*)$  is increasing in  $\sigma_e^2$  and  $\sigma_n^2$  and decreasing in  $\rho\sigma_e\sigma_n$ .

**Remark 3.** ETFs characterized by larger exposure to non-fundamental demand shocks (large values of  $\sigma_e^2$ ,  $\sigma_n^2$ , or both) and larger differences in sensitivities to non-fundamental demand shocks (large differences in  $\sigma_e$  and  $\sigma_n$ ) have more volatile flows.

Remark 3 implies that ETFs with volatile flows are most symptomatic of non-fundamental demand shocks, particularly if the investor clientele that trade the ETF shares and the ETF underlying assets are sufficiently different (i.e., large differences in  $\sigma_e$  and  $\sigma_n$ ).

Having outlined the model and having demonstrated the mechanism, it is worthwhile to place our model in the fund flows literature. The most natural benchmark model is that of Berk and Green (2004).<sup>17</sup> Berk and Green (2004) provides a rational explanation for the “fund-flow anomaly.”<sup>18</sup> Specifically, in the model, fund managers have unobservable skill to earn abnormal returns, funds experience diminishing returns to fund size, and investors with perfectly elastic capital learn about managerial skill via realized performance. As such, after performance is revealed, investors update their beliefs about each fund manager’s skill and reallocate capital such that any expected abnormal returns are competed away. Thus, in Berk and Green (2004), mutual

<sup>16</sup> While the fundamental component does not directly affect ETF flows, the non-fundamental component can be correlated with the fundamental component (e.g., under- or over-reaction). See Section 7 of the Internet Appendix for additional discussion.

<sup>17</sup> See also the models of Pástor and Stambaugh (2012), Brown and Wu (2016), and Brown and Davies (2017).

<sup>18</sup> The “fund-flow anomaly” is empirical evidence that shows mutual fund investors chase realized performance (i.e., inflows after positive relative performance and outflows after negative relative performance), but this return-chasing behavior is unrelated to the fund’s subsequent performance. See Ippolito (1992), Chevalier and Ellison (1997), and Sirri and Tufano (1998).

fund flows reflect the evolution of investors' beliefs regarding managerial skill.

Our model is distinct from that of Berk and Green (2004) for one primary reason: ETFs are passively managed. As such, realized performance is unrelated to managerial skill and cannot reflect the evolution of rational beliefs. However, ETF flows in our model do share one important similarity with the mutual fund flows in Berk and Green (2004); they both reflect competition among rational agents. In Berk and Green (2004), mutual fund flows reflect rational investors competing away expected abnormal returns arising from managerial skill. In our model, ETF flows reflect rational authorized participants competing away relative mispricing arising from non-fundamental demand.

Using the equilibrium ETF flow  $\Delta^*$ , we solve for the equilibrium  $t = 2$  prices and the corresponding equilibrium ETF premium  $\psi_2$ , ETF fundamental mispricing  $\varphi_2$ , and the NAV fundamental mispricing  $\alpha_2$ . Hereafter, we drop the time subscript 2 and add a superscript of  $*$  to highlight that the ETF premium, ETF fundamental mispricing, and the NAV fundamental mispricing are equilibrium outcomes.

**Proposition 1.** *The  $t = 2$  equilibrium ETF premium is given by,*

$$\lim_{N \rightarrow \infty} \psi^* = \lim_{N \rightarrow \infty} \left(1 - \frac{N}{N+1}\right) (\epsilon^{etf} - \epsilon^{nav}) = 0. \quad (11)$$

*The  $t = 2$  equilibrium ETF fundamental mispricing and NAV fundamental mispricing are given by,*

$$\lim_{N \rightarrow \infty} \varphi^* = \lim_{N \rightarrow \infty} \alpha^* = \epsilon^{etf} \frac{\lambda}{\lambda + \eta} + \epsilon^{nav} \frac{\eta}{\lambda + \eta}. \quad (12)$$

While we focus on the limiting case in which  $N \rightarrow \infty$ , Equation 11 shows that, for a finite  $N$ , the equilibrium ETF premium is linear in the difference of the two non-fundamental demand shocks (i.e.,  $\epsilon^{etf} - \epsilon^{nav}$ ), similar to the ETF flow.

**Remark 4.** In the absence of perfect competition, ETF premia changes are symptomatic of non-fundamental demand distortions.

Remark 4 mirrors Remark 2: observed ETF premia changes are symptomatic of non-fundamental demand shocks if  $N$  is finite. However,  $\psi^*$  is decreasing in  $N$  and goes to zero in the limit while  $\Delta^*$  goes

to a finite quantity in the limit. Thus, if ETF flows and ETF premia are measured with error, the signal-to-noise ratio in using  $\Delta^*$  to signal non-fundamental demand is increasing in  $N$  and the signal-to-noise ratio in using  $\psi^*$  to signal non-fundamental demand is decreasing in  $N$ . In our empirical analysis, we attempt to identify fundamental mispricing using both ETF flows and ETF premia changes. We find that ETF flows are strong signals of non-fundamental demand, while ETF premia changes are not, consistent with the authorized participant market being highly competitive.

**Remark 5.** If  $\lambda > 0$ , then the non-fundamental demand shock  $\epsilon^{etf}$  may be transmitted to the underlying assets via the ETF primary market mechanism. If  $\eta > 0$ , then the non-fundamental demand shock  $\epsilon^{nav}$  may be transmitted to the ETF shares via the ETF primary market mechanism.

Remark 5 implies two potential sources of price distortions for the ETF share price and the ETF underlying asset prices. The first source is straightforward, that is, the latent demand shocks themselves:  $\epsilon^{etf}$  distorts the ETF share price and  $\epsilon^{nav}$  distorts the underlying asset prices. The second source, which is more subtle, is a transmission mechanism via the primary market: arbitrageurs trade against relative mispricing until it dissipates, implying arbitrage trades have price impact. Thus, if a price distortion occurs on one side of the ETF basket (in either the ETF shares or the underlying assets), subsequent arbitrage trades transmit the price distortion to the other side of the basket. In Section 8 of the Internet Appendix, we provide a test for identifying these two different sources and we show empirically that both sources distort ETF share prices and ETF underlying asset prices.

Proposition 1 also shows that the equilibrium ETF fundamental mispricing and the equilibrium NAV fundamental mispricing are a weighted average of the two non-fundamental demand shocks in which the weight on the ETF demand shock is  $\frac{\lambda}{\lambda+\eta}$  and the weight on the NAV demand shock is  $\frac{\eta}{\lambda+\eta}$ . When  $\eta$  and  $\lambda$  are equal, the fundamental mispricing is a simple average of  $\epsilon^{etf}$  and  $\epsilon^{nav}$ .

At  $t = \textit{long term}$ , we assume the ETF share price and underlying asset prices converge to their latent fundamental value. That is, while short-run responses to fundamental mispricing are inelastic, long-run

responses are highly elastic (e.g., due to slow-moving capital as in Duffie, 2010).

**Remark 6.** ETF flows almost always signal a fundamental mispricing that subsequently reverses.

Remark 6 highlights the primary motivation for our empirical analysis. While *relative* pricing is efficient ( $\psi^* = 0$ ), ETF flows reveal *fundamental* mispricing ( $\varphi^* = \alpha^* \neq 0$ ) that reverses in time (the long-term price reversion is  $-\varphi^* = -\alpha^*$ ).<sup>19</sup> In practice, this reversion may be fast if traders are willing and able to exploit the profitable trade quickly. Conversely, the reversion may be slow if traders are unwilling or unable to exploit the trade due to market frictions or risks. The long-term reversion may also be obscured by fundamental price movements that are correlated with ETF flows. So while the reversion would still exist, its magnitude may be small and difficult to detect. Whether or not the fundamental mispricing is observable is an empirical question and the subject of our study.

Finally, how ETF flows are related to future returns depends on whether ETF shares or the underlying assets are more sensitive to non-fundamental demand shocks. While our model is agnostic regarding the direction of the relation, the sign of the relation is given by the slope coefficient from a regression of long-term returns on ETF flows (assuming  $\rho = 1$ ),

$$\frac{Cov(-\varphi^*, \Delta^*)}{Var(\Delta^*)} = \frac{Cov(-(\lambda\epsilon^{etf} + \eta\epsilon^{nav}), \epsilon^{etf} - \epsilon^{nav})}{Var(\epsilon^{etf} - \epsilon^{nav})} \quad (13)$$

$$= \frac{(\sigma_n - \sigma_e)(\lambda\sigma_e + \eta\sigma_n)}{Var(\epsilon^{etf} - \epsilon^{nav})}, \quad (14)$$

with the sign on the coefficient being determined by  $\sigma_n - \sigma_e$ .

**Remark 7.** If ETF share demand is relatively more sensitive to non-fundamental demand shocks as compared to the ETF underlying asset demand, that is,  $\sigma_e > \sigma_n$ , then ETF flows negatively predict returns. If  $\sigma_n > \sigma_e$ , then ETF flows positively predict returns.

<sup>19</sup> Note, as can be seen in Equation 12, it is possible that the fundamental mispricing is zero even if there is a non-fundamental demand shock, for example, when  $\epsilon^{etf}$  and  $\epsilon^{nav}$  exactly offset.

**Remark 8.** Because  $\varphi^* = \alpha^*$ , return predictability of ETF share returns and NAV returns should be qualitatively the same.

Remark 7 and Remark 8 provide two insights to guide the subsequent empirical analysis. According to Remark 7, the sign on the coefficient from return predictability regressions provides insights into whether the ETF shares or the underlying assets are more sensitive to non-fundamental demand shocks. In our empirical tests, we consistently find a statistically significant negative coefficient, suggesting that ETF share demand is relatively more sensitive to non-fundamental demand shocks. According to Remark 8, our results should be approximately the same using ETF share returns or NAV returns as the dependent variable, which we find to be the case.

As discussed at the beginning of this section, the insight that ETF flows must imply a non-fundamental distortion is not driven by the setup or assumptions. However, there are several assumptions and modeling conveniences used which limit what we can learn about the ETF market. Notably, (i) we assume that the opportunity cost of arbitrage capital is zero, (ii) we do not model the authorized participants' trades in a dynamic framework, and (iii) we ignore the possibility that restoring relative price efficiency in one ETF may generate mispricing in a different ETF. Considering the possibility that arbitrage capital is costly implies that some arbitrage opportunities will not be large enough to attract authorized participants. Moreover, if the cost of arbitrage capital is stochastic, ETF flows and changes in ETF premia may reflect innovations to this cost.<sup>20</sup> In regards to our model's timing, we implicitly assume that authorized participants treat a relative mispricing as a one-shot game. In reality, authorized participants may trade against relative pricing while taking into consideration the possibility of future trades and the future actions of their competitors. Finally, we assume that authorized participants focus on a single arbitrage opportunity. In reality, there may be dozens of arbitrage opportunities at a given moment and an authorized participant's optimal trading is more com-

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<sup>20</sup> Importantly, in our empirical analysis we address that arbitrage activity is an equilibrium outcome and it reflects, among other things, the cost of arbitrage capital and macroeconomic conditions. Specifically, we include both date fixed effects and fund-level controls in our panel regressions.

plicated than what we study. Thus, while our model is simple and insightful, the model has limitations that merit future research.

### 3. Data

We study the ability of ETF flows and ETF premia changes to predict subsequent returns using data from several sources. From Bloomberg, we get daily data on ETF share prices, NAVs, shares outstanding, and trading volumes.<sup>21</sup> Each date, we calculate ETF premia (discounts) as the difference between each ETF's price and its NAV and report the value as a percentage of NAV. We merge this data with information from CRSP including Lipper Codes and ETF returns, as well as holdings data for many of our sample ETFs. To calculate risk-adjusted measures of returns, we add information on the Fama-French three-factor (Fama and French, 1993), Fama-French three-factor plus momentum (Carhart, 1997), and Fama-French five-factor (Fama and French, 2015) models from Kenneth French's website, as well as information on the Hou-Xue-Zhang four-factor model (Hou, Xue and Zhang, 2015) provided by Lu Zhang.

Table 1 displays a time-series count of the number of ETFs in our sample. The ETF market has grown rapidly over the last decade, and by the end of 2016, our sample includes 1,515 unique ETFs.<sup>22</sup> To mitigate the impact of illiquidity and possible non-synchronous prices due to infrequent trading, we limit our sample to ETFs with at least \$50 million in assets. 27% of ETFs are excluded using the \$50 million threshold, but they collectively account for less than 1% of market capitalization. To focus on ETFs with active primary markets, we also consider a sample of ETFs that are flagged as "mature" once they exceed the \$50 million threshold and experience a month in which at least one-half of the trading days had some share creation/redemption activity. As shown in

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<sup>21</sup> A number of ETFs have anomalous data on prices and shares outstanding that appear to be incorrect. We clean the data by removing the anomalies that are not verifiable via other data sources. See Internet Appendix Section 9 for more details on database construction and cleaning. Furthermore, Ben-David, Franzoni and Moussawi (2018) suggest that Bloomberg provides the most accurate daily ETF data.

<sup>22</sup> While we have data on 1,707 ETFs at the end of the 2016, we require at least twelve months of observations to be included in our sample. As a result, the ETFs introduced in 2016 are not in our sample.

Table 1, this filter removes approximately half of the remaining ETFs, but only reduces the total market capitalization by 10%.

In several of our tests, we split our mature sample into two subsets: unleveraged mature ETFs and leveraged mature ETFs. There are good reasons to split unleveraged and leveraged ETFs into subsets. First, leveraged ETFs are characterized by relatively more extreme flows as compared to unleveraged ETFs. For example, leveraged ETFs represent only 15.0% of the monthly ETF observations in our mature sample, but they represent 33.2% of observations in the top and bottom deciles of our portfolio sorts. Second, leveraged ETFs are uniquely tailored for short-horizon traders who want to make magnified bets on the performance of a benchmark index. As such, leveraged ETFs are characterized by high share turnover and low institutional ownership relative to unleveraged ETFs.<sup>23</sup> Third, leveraged ETF shares are backed by derivative contracts (e.g., total return swaps) and share creations/redemptions are performed using cash. Conversely, almost all unleveraged ETF shares are backed by an underlying basket of securities that replicate the benchmark index (either through full replication or an optimized replication to avoid illiquid securities) and they use in-kind creations/redemptions. The final two columns of Table 1 provide the time series counts of the unleveraged mature sample and the leveraged mature sample. Early in the sample, leveraged mature ETFs represent only a small percentage of the mature ETF sample, both in terms of count and total market capitalization. By the end of the sample, leveraged mature ETFs represent a larger percentage of the mature ETF sample count but they remain only a small percentage of total market capitalization.

Table 2 displays summary statistics for six samples: the entire ETF sample, the sample of \$50M+ ETFs, the mature sample of ETFs, the unleveraged mature and leveraged mature samples, and a sample of unleveraged ETFs with high primary market activity (which are introduced and studied later in the paper). In comparing the entire ETF sample to the \$50M+ sample, the \$50M+ sample is generally representative of the entire sample with \$50M+ ETFs exhibiting better liquidity (tighter bid-ask spreads and greater short interest percentages) and experiencing more frequent and larger flows. The two samples are nearly identical in terms of the Lipper Category percentages. In comparing

<sup>23</sup> See Davies (2020) for additional detail.

the \$50M+ ETFs to the mature ETFs, the mature sample ETFs are larger and generally experience more trading and better liquidity; mature ETFs have more shares outstanding, more turnover, and tighter bid-ask spreads. In terms of Lipper Categories, the two samples are fairly similar, but mature ETFs tend to be more focused on equities and less focused on bonds and international assets.

Table 2 shows that the mature unleveraged ETFs and mature leveraged ETFs greatly differ. The leveraged sample exhibits considerably more trade volume, both in shares and as a percentage of shares outstanding, consistent with leveraged ETFs being used primarily by short-horizon traders. Furthermore, while the percentages of days with share creation/redemption activity are approximately the same, the magnitude of flows is over twice as large in the leveraged sample.

Motivated by our theoretical model, we examine the relation between signals of non-fundamental demand shocks (i.e., ETF flows and ETF premia changes) and subsequent returns. We calculate ETF flows and ETF premia changes at a monthly frequency and we avoid higher frequency measures for several reasons. First, the accounting standards for share creation/redemption activity vary across ETFs — some funds use  $T + 1$  accounting (i.e., they register the share creation activity the day after it occurs) while other funds use  $T$  accounting. Moreover, these accounting standards have changed over time, and the change from  $T + 1$  to  $T$  accounting, or vice versa, is not public.<sup>24</sup> Second, there is evidence that authorized participants strategically delay creating or redeeming shares to take advantage of failure-to-deliver rules at clearing houses. Evans et al. (2019) describes how authorized participants can wait until  $T + 6$  to create new shares and avoid costs associated with short-selling. Third, arbitrage activity itself creates price pressure in the ETF and underlying assets.<sup>25</sup> To avoid the effects of price pressure from arbitrage activity, and instead emphasize longer-term return predictability due to non-fundamental demand shocks, we measure ETF flows at the monthly horizon.

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<sup>24</sup> See Staer (2016) for additional details.

<sup>25</sup> Ben-David, Franzoni and Moussawi (2018) show that arbitrage activity itself leads to increased volatility in the underlying assets due to price pressure from ETF flows. See also Fulkerson and Jordan (2013). Similarly, Internet Appendix Table IA21 shows that in our sample, large ETF premia changes lead to predictable ETF and NAV returns (in opposite directions) over the following day.

#### 4. Non-Fundamental Demand and Return Reversals

Our model shows that ETF flows and ETF premia changes signal relative non-fundamental demand shocks that generate mispricing between the ETF shares and the ETF underlying assets.<sup>26</sup> The model also shows that ETF flows and ETF premia changes provide conditioning information to identify fundamental mispricing. However, the model is agnostic regarding the magnitude of the fundamental mispricing and the horizon at which it reverses. In this section, we analyze the relation between lagged flows/premia changes and future returns in the cross-section. Under the null hypothesis, there should be no return predictability from either ETF flows or ETF premia changes. That is, any fundamental mispricing (i.e., a risky arbitrage) is either too small to be measured or is quickly exploited by market participants.

To measure ETF flows, we calculate creation and/or redemption activity in a given ETF. Formally, we define ETF flow as the percentage change in ETF shares outstanding for fund  $j$  at time  $t$ ,

$$ETFFlow_{j,t} = \frac{SharesOutstanding_{j,t}}{SharesOutstanding_{j,t-1}} - 1. \quad (15)$$

To measure ETF premia changes for ETF  $j$ , we calculate the ETF premium at time  $t$  and subtract the ETF premium at time  $t - 1$ ,

$$ETFPremChange_{j,t} = (p_t/\pi_t - 1) - (p_{t-1}/\pi_{t-1} - 1), \quad (16)$$

in which  $p_t$  is the ETF share price at time  $t$  and  $\pi_t$  is the NAV per share at time  $t$ .

We sort ETFs into portfolios based on either  $ETFFlow_{j,t}$  or  $ETFPremChange_{j,t}$  to test whether these signals of relative non-fundamental demand shocks are related to future ETF performance. In all of our portfolio sorts, we sort based on characteristics at a monthly level, preventing time trends and differences in sample size from driving our results. We measure ETF performance using ETF returns from the months following portfolio formation. For the sorts using ETF flows, ETFs with the most positive flows (i.e., share creations) in the past month are sorted into Decile 10, and ETFs with the most negative

<sup>26</sup> ETF premia changes only signal non-fundamental demand shocks if the market for authorized participants is not perfectly competitive.

flows (i.e., share redemptions) are sorted into Decile 1.<sup>27</sup> For the sorts using ETF premia changes, ETFs with the largest increase in average premia in the past month are sorted into Decile 10 and ETFs with the largest decrease in average premia are sorted into Decile 1.

Figure 2 plots the value-weighted raw ETF returns from a long-short trading strategy that goes long the ETFs in Decile 1 and goes short the ETFs in Decile 10. In each plot, the horizontal axis represents the number of months following the formation of the long-short portfolio and the vertical axis represents the portfolio's raw return. At each monthly data point, error bars are included to provide the 95% confidence interval. Plot (a) and Plot (b) depict the trading strategy raw returns for the mature ETF sample, based on ETF flows and based on ETF premia changes. Plot (c) and Plot (d) use the mature leveraged ETFs and Plot (e) and Plot (f) use the mature unleveraged ETFs.

The plots illustrate four findings that guide our subsequent analysis. First, ETF *flows* appear to provide cross-sectional return predictability: in the mature ETF sample, the mature leveraged ETF sample, and the mature unleveraged ETF sample, raw returns appear to be positive and significantly different than zero (albeit, over different horizons). Second, ETF flows are negatively related to subsequent returns which suggests, according to Remark 7, that ETF shares are relatively more sensitive to non-fundamental demand shocks on average. Third, ETF *premia changes* do not appear to predict cross-sectional returns. While the returns from conditioning on ETF premia changes are generally positive, they are not statistically different from zero. As such, ETF flows are better signals for non-fundamental demand shocks than ETF premia changes. This is consistent with our model's prediction if the primary market for ETFs is highly competitive and premia are measured with noise. In what follows, we focus exclusively on ETF flows, but we include additional analysis in Internet Appendix Table IA8 using ETF premia changes. Fourth, the return predictability horizons differ significantly between mature leveraged ETFs and mature unleveraged ETFs. Almost all returns in the trading strategy using

<sup>27</sup> Because  $ETFFlow_{j,t}$  and  $ETFPremChange_{j,t}$  are both measured as percentage changes, it is possible that smaller ETFs are more likely to be sorted into the extreme deciles and thereby drive the results of our portfolio sort tests. Table IA12 in the Internet Appendix shows this is not the case by first sorting ETFs by size (market capitalization) before sorting into flow deciles. Large ETFs show strong return predictability, particularly for mature, unleveraged ETFs.

mature leveraged ETFs are earned in the first month. Conversely, the returns in the trading strategy using mature unleveraged ETFs are primarily earned in months two through six.

Motivated by the plots in Figure 2, Panel A of Table 3 displays raw returns for portfolios formed using lagged ETF flows.<sup>28</sup> We construct equal-weighted and value-weighted (based on ETFs' AUMs) long-short portfolios and report portfolio returns at one-, three-, and six-month horizons. Beginning with our broadest samples, the \$50M+ and mature ETF samples exhibit statistically significant long-short portfolio returns at the one-, three-, and six-month horizons (to account for overlapping return periods, we use Newey-West standard errors with the lag equal to the return horizon in months). One-month long-short portfolio returns range from 1.1% to 2.0% monthly (which compounds to 14.5% to 27.2% annually), three-month returns range from 2.3% to 2.7% quarterly (9.7% to 11.4% annually) and six-month returns range from 3.6% to 3.9% semiannually (7.3% to 7.9% annually). Collectively, these results show that ETF flows predict future returns in the cross-section.

To examine the differences in return predictability horizons shown in Figure 2, we analyze mature leveraged and unleveraged ETFs separately. Beginning with the mature leveraged ETF results, one-month long-short portfolio returns are statistically significant and range from 4.4% to 4.5% (67.8% to 68.7% annually).<sup>29</sup> However, over three- and six-month horizons, the leveraged ETF returns are flat relative to what is earned in the first month and are not significantly different from zero. Turning to the mature unleveraged ETF results, returns do not exhibit predictability at a one-month horizon. However, at the three-month horizon, the value-weighted, long-short portfolio earns statistically significant returns of 1.2% (4.8% annually). At the six-month horizon both

<sup>28</sup> In Internet Appendix Section 1, we replicate Table 3 using risk-adjusted returns from the Fama-French three-factor model (Fama and French, 1993), the four-factor Carhart (1997) model, the Fama-French five-factor model (Fama and French, 2015), and the Hou-Xue-Zhang four-factor model (Hou, Xue and Zhang, 2015). See Tables IA1, IA2, IA3, and IA4.

<sup>29</sup> In Internet Appendix Tables IA5 and IA6, we show that our leveraged ETFs results are not driven by the optionality embedded in leveraged ETFs. Specifically, leveraged ETFs follow a dynamic trading strategy that synthesizes an Asian option, so their realized returns depend on the realized volatilities and realized returns of the underlying indexes. To ensure our results are not driven by this feature, we de-leverage these ETF returns. Our conclusions remain unchanged.

the equal-weighted and value-weighted portfolios earn statistically significant returns of 1.2% (2.4% annually) and 2.0% (4.0% annually).

Our model provides two reasons why leveraged ETFs show strong return predictability. Remark 3 suggests that the best measures of non-fundamental demand shocks occur in ETFs in which (i) flows are volatile, and (ii) there are different trader clienteles transacting the ETF shares and the ETF underlying assets. Leveraged ETFs meet both conditions. First, Table 2 shows that leveraged ETFs have over twice as much creation/redemption activity as unleveraged ETFs. Second, while traders purchase leveraged ETF shares for short-horizon, magnified exposure to market benchmarks, the shares are backed by derivative securities (e.g., total return swaps) which are transacted for many other purposes such as risk management and hedging. Furthermore, any trader can purchase leveraged ETF shares without special authorizations (even in some retirement accounts like 401(k)s), while the derivative securities are traded almost exclusively among institutions. Thus, there is a wedge between the clienteles that trade leveraged ETF shares and that trade the underlying derivative securities. One clientele is largely retail and motivated by short-horizon, leveraged exposure and the other clientele is largely institutional and motivated by multiple purposes including hedging.

Remark 3 is not specific to leveraged ETFs. ETFs with active primary markets feature volatile flows and different clienteles owning the ETFs and their underlying assets. Accordingly, we perform an additional test on the mature unleveraged ETF sample in Panel B of Table 3. The additional test provides robustness in showing that our return predictability results are not driven exclusively by leveraged ETFs. To focus on ETFs with active primary markets, we first sort the sample into terciles based on the number of days in the month for which there was any share creations/redemptions.<sup>30</sup> We refer to the top tercile as high activity ETFs. Within each tercile, we sort ETFs into deciles according to ETF flows. Panel B shows stronger return predictability for high activity ETFs as compared to the full sample of unleveraged ETFs in Panel A, both in terms of economic magnitudes and statistical significance. The high activity ETFs exhibit statistically significant return predictability at both three-month and six-month horizons. For

<sup>30</sup> In Internet Appendix Table IA9, we replicate this analysis by sorting on flow volatility instead of activity. While the results are noisier, our conclusions remain unchanged.

equal- and value-weighted portfolios, the three-month long-short portfolio returns are 1.2% (5.0% annually) and 1.5% (6.3% annually), and the six-month returns are 2.5% (5.1% annually) and 3.3% (6.8% annually). The analysis shows that, while the results are most pronounced in the mature leveraged ETF sample, the results extend to unleveraged ETFs as well.<sup>31</sup>

The horizons at which the returns persist are also of interest. The existing literature on investor flows typically finds evidence of long-horizon predictability. For example, Frazzini and Lamont (2008) document evidence of return predictability at a horizon of several years. Instead, we find return predictability over the one- to six-month horizons. Table 3 shows that the non-fundamental demand shocks measured by flows in leveraged ETFs generate short-lived dislocations that correct over one month, while non-fundamental demand shocks measured by flows in unleveraged ETFs generate longer-lived dislocations that take several months to remedy. The difference in horizons for the return predictability could be due to several factors. For example, leveraged ETFs and unleveraged ETFs may attract different investor clienteles who are exposed to different types of non-fundamental demand. Alternatively, market participants may face different risks in exploiting the fundamental mispricing signaled by leveraged ETF flows as compared to the fundamental mispricing signaled by unleveraged ETF flows.

Return predictability from ETF flows is related to, but distinct from, the large literature showing that mutual fund flows contain information about future asset returns. For example, Ben-Rephael, Kandel and Wohl (2012) shows that flows aggregated across mutual funds can be used to measure non-fundamental demand. To test whether our findings are distinct from theirs, we orthogonalize *ETFFlow* to US aggregate net equity fund flows from Ben-Rephael, Kandel and Wohl (2012). We document in Internet Appendix Table IA7 that *ETFlow* is not simply measuring a known source of return predictability in a different way. The coefficient estimates and standard errors are consistent with those in Table 3 and lead to the same conclusions. In other words, the sig-

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<sup>31</sup> Internet Appendix Tables IA10 and IA11 analyze return predictability separately for broad equity, sector equity, bond, international and commodity ETFs. The results show that ETF categories with more active primary and secondary markets show more return predictability, consistent with the results for leveraged ETFs and unleveraged, high activity ETFs.

nal of non-fundamental demand from ETF flows is different from that found in aggregate mutual fund flows.

Remark 8 predicts that return predictability should be similar using either ETF returns or NAV returns. Table 4 uses NAV returns and confirms this prediction showing very similar results to the ETF returns in Table 3.<sup>32</sup> In addition to validating our model, finding similar return predictability for ETF and NAV returns reinforces that the return predictability is not due to the arbitrage activity itself (which puts opposite pressure on the ETF and NAV). Rather, our findings are consistent with long-term price reversals following non-fundamental demand shocks that are signaled by arbitrage activity.

#### 4.1 Panel Regressions

To examine the robustness of our portfolio sorts, we estimate the panel regression:

$$Performance_{j,t+h} = \beta FlowMeasure_{j,t} + \gamma_t + \delta V_{j,t} + \epsilon_{j,t+h}, \quad (17)$$

in which  $Performance_{j,t+h}$  is a measure of ETF  $j$ 's performance (i.e., raw return including distributions or abnormal returns using a risk model) at horizon  $h$ ,  $h$  is either one month, three months, or six months,  $FlowMeasure_{j,t}$  is either the set of indicator variables  $Decile_{j,d,t}$  for whether ETF  $j$  is in decile portfolio  $d$  in period  $t$  (from sorting on  $ETFFlow_{j,t}$ ) or the continuous measure  $ETFFlow_{j,t}$ ,  $\gamma_t$  are date fixed effects, and  $V_{j,t}$  are lagged fund controls including two lags of ETF returns, ETF premium, ETF share volume, and ETF market capitalization. To account for overlapping return periods, we calculate Driscoll and Kraay (1998) standard errors with the lag equal to the return horizon in months.

We calculate abnormal returns by regressing monthly ETF returns on Fama-French three-factor plus momentum (Carhart, 1997) factor returns:

$$Ret_{j,t+h} = \alpha + \Gamma X_{t+h} + \eta_{j,t+h}, \quad (18)$$

in which  $X_{t+h}$  is a vector of factor returns for time  $t$  at horizon  $h$  and the residual,  $\eta_{j,t+h}$ , represents the abnormal return. Importantly,

<sup>32</sup> Moreover, Internet Appendix Section 6 shows that our results extend to the individual stock level.

date fixed effects help differentiate our results from several existing measures that have been used as proxies for non-fundamental demand, including aggregate sentiment proxies (e.g., Baker and Wurgler, 2007) and trading frictions like intermediary funding liquidity (e.g., He, Kelly and Manela, 2017).<sup>33</sup> In addition, using two lags of ETF return controls for return predictability due to known sources of return-induced non-fundamental trades (i.e., extrapolation or contrarian trading). As such, our results are more likely to isolate noise that is distinct from other non-fundamental demand proxies.

Starting at the one-month horizon, Column (1) of Table 5 shows that Decile 10 ETFs (those with the most inflows) underperform, in raw returns, Decile 1 ETFs (the omitted group and those with the most outflows) by 186 bps per month (24.8% annually), which is significant at a 1% p-value threshold. Column (2) shows that Decile 10 ETFs underperform, in abnormal returns, Decile 1 ETFs by 79 bps (9.9% annually), which is significant at a 1% p-value threshold. Column (3), which uses a continuous measure of ETF flows, shows a negative coefficient on  $ETFFlow_{j,t}$ , but it is not statistically significant. Comparing Columns (1) and (2) to Column (3) suggests a non-linear relation between lagged ETF flows and subsequent performance.

Turning to the three-month horizon, Column (4) shows that Decile 10 ETFs underperform, in raw returns, Decile 1 ETFs by 210 bps per quarter (8.7% annually) which is significant at a 1% p-value threshold. Column (5) shows that Decile 10 ETFs underperform, in abnormal returns, Decile 1 ETFs by 76 bps per quarter (3.1% annually), which is significant at a 5% p-value threshold. Column (6) uses a continuous measure of ETF flows and, while the coefficient on  $ETFFlow_{j,t}$  is negative, it is not statistically significant.

Finally, Columns (7)-(9) consider performance measures at a six-month horizon. Column (7) shows that Decile 10 ETFs underperform, in raw returns, Decile 1 ETFs by 375 bps per half year (7.6% annually), which is significant at a 1% p-value threshold. Column (8) shows that Decile 10 ETFs underperform, in abnormal returns, Decile 1 ETFs by 158 bps per half year (3.2% annually), which is significant at a 5% p-value threshold. Column (9) mirrors Column (3) and Column (6);

<sup>33</sup> Using a panel regression with date fixed effects also alleviates potential concerns of a Stambaugh (1999) bias. Furthermore, ETF flows are neither highly persistent nor correlated with contemporaneous returns.

while the coefficient on  $ETFFlow_{j,t}$  is negative, it is not statistically significant. In Internet Appendix Table IA13, we show that our results are qualitatively similar using NAV returns in place of ETF returns, consistent with Remark 8.<sup>34</sup>

Table 5 confirms the long-short portfolio results in Table 3 and both tables document an economically meaningful and statistically significant relation between ETF flows and subsequent returns. The analysis is consistent with ETF flows' signaling non-fundamental demand shocks that push asset prices away from fundamentals. This fundamental mispricing reverses over the span of one to six months.

#### 4.2 Trading Strategy Performance

To investigate the practical implications and the economic significance of our results, we evaluate the performance of several trading strategies that condition on ETF flows using the same portfolio formation process. Table 6 details the performances of long-short trading strategies using three ETF samples, (i) mature ETFs, (ii) leveraged ETFs, and (iii) high activity unleveraged ETFs (i.e., those in the top tercile of primary market activity), over one-month and six-month horizons. The value-weighted one-month horizon strategy turns over monthly based on the prior month's flows. The six-month horizon strategy is constructed by equally-weighting the six most recent one-month horizon portfolios. Therefore, each month, the oldest one-month portfolio rolls out of the set of six and the newest one-month portfolio rolls in. For each ETF sample and at each horizon, we report the mean annual return, the annualized standard deviation of monthly returns, the annualized Sharpe ratio, and the maximum monthly loss.

Panel A of Table 6 presents the results for our entire ten-year sample. For the mature ETF sample, the one-month strategy's mean annual return is 11.96% and the six-month strategy's mean annual return is 8.03%. For the leveraged ETF sample, the mean annual returns are 27.21% and 8.08%, and for the high activity unleveraged ETF sample,

<sup>34</sup> In Table IA14 of the Internet Appendix, we show that these results hold after we orthogonalize  $ETFFlow$  to US aggregate net equity fund flows from Ben-Rephael, Kandel and Wohl (2012). Tables IA15 and IA16 show that these results continue to hold after accounting for the optionality embedded in leveraged ETFs. Tables IA17, IA18 and IA19 show that, for sub-samples of leveraged and unleveraged ETFs, panel regression results are consistent with the portfolio sort results reported in Tables 3 and 4.

the mean annual returns are 3.07% and 6.05%. The samples' mean annual returns are consistent with the earlier findings showing that the leveraged ETF strategy predicts large return reversals over a short horizon while the high activity unleveraged ETF strategy predicts more moderate return reversals over a longer horizon. The strong performance in the leveraged ETF sample, relative to the mature sample and the high activity unleveraged sample, is not without risk. The standard deviation of returns is 74.42% and 39.76% in the leveraged ETF sample, which corresponds to Sharpe ratios of 0.37 and 0.20. In comparison, the standard deviation of returns in the mature ETF sample is smaller, leading to stronger Sharpe ratios; the one-month horizon and six-month horizon annual Sharpe ratios are 0.60 and 0.99. For the high activity unleveraged ETF sample, the Sharpe ratios are the lowest for the one-month strategy (0.22), but are higher for the six-month strategy (0.82).

Panel B of Table 6 presents the results over the sample period of 2007-2011. During this window, in which the 2008 Financial Crisis falls, the mature ETF sample dominates the leveraged and high activity unleveraged samples with respect to Sharpe ratios. For the one-month strategy, the mature sample achieves a Sharpe ratio of 0.75 while the leveraged sample and high activity unleveraged sample earn Sharpe ratios of 0.23 and 0.51. For the six-month strategy, the mature sample achieves a Sharpe ratio of 1.14 and the leveraged and high activity unleveraged samples achieve Sharpe ratios of  $-0.24$  and 1.06. Panel C presents the results over the second half of our sample, 2012-2016. Again, the mature sample outperforms the leveraged and high activity unleveraged samples in terms of Sharpe ratios, both for the one-month strategy and the six-month strategy. The mature sample also outperforms in terms of maximum monthly loss.

Table 6 provides two insights. First, while return predictability is strongest in the mature leveraged sample, it comes with two undesirable features: (i) the volatility of returns is 3-7 times larger than the volatility in the mature sample and the high activity unleveraged sample and (ii) the increase in volatility does not correspond to proportionally greater returns, leading to lower overall Sharpe ratios. Second, both mean annual returns and Sharpe ratios are consistently higher in the mature ETF sample than in the sub-samples of leveraged and high activity unleveraged ETFs. As such, there appears to be a diversifi-

cation benefit in building the ETF portfolio using both leveraged and unleveraged ETFs.

## 5. ETF Investor Performance

The analyses in Section 4. suggest that non-fundamental demand shocks, measured by ETF flows, create relative mispricing among ETFs; those ETFs with the greatest inflows underperform those with the greatest outflows. In this section, we examine how the relation between non-fundamental demand shocks and returns affects investor performance. Specifically, for each ETF, we quantify the costs (if any) for investors due to a negative relation between ETF flows and subsequent returns. To do so, we consider two measures of ETF investor performance and examine ETFs on a fund-by-fund basis.

First, we examine each ETF's internal rate of return (IRR), which considers both inflows and outflows to the ETF (see Dichev, 2007 and Dichev and Yu, 2011). Unlike the return on a single ETF share, the IRR measures the timing impact of ETF flows and it provides the return that a representative investor would have earned if she held all shares and was responsible for all ETF flows.

Second, we examine a measure we call *share-growth-adjusted return* (SGAR). SGAR measures the dynamic performance of an investor that allocates capital between ETF shares and a risk-free asset based on the prior month's flows. To calculate the SGAR for each ETF, we take its return series  $\mathbf{r} = \{r_1, \dots, r_T\}$  and its one-period-lagged share growth series  $\mathbf{g} = \{g_0, \dots, g_{T-1}\}$  and perform the following calculation,

$$\text{SGAR} = \left( \prod_{\tau=1}^T ((1 + r_\tau)(1 + g_{\tau-1}) - (1 + r_{f,\tau})g_{\tau-1}) \right)^{12/T} - 1, \quad (19)$$

in which  $r_{f,\tau}$  is the risk-free rate at time  $\tau$ .<sup>35</sup> SGAR is a pseudo portfolio return that captures the notion that share creations and redemptions have a leverage-like effect on total return; the SGAR puts more weight on returns after inflows and less weight on returns after outflows. SGAR assumes that capital may be invested in the risk-free asset (negative values of  $g_{\tau-1}$ ) and may also be borrowed at the risk-free rate (positive values of  $g_{\tau-1}$ ).

<sup>35</sup> We get the monthly risk-free rate from Kenneth French's website.

The IRR and SGAR measures differ in important ways and each measure has its own strengths and weaknesses. IRR is sensitive to the correlation of flows and returns, regardless of the number of months separating a particular flow from a particular return. As such, IRR captures correlations between flows and returns without restrictions on the time series properties, allowing identification of fundamental mispricings that take several months to reverse. However, this flexibility comes with a cost as one cannot disentangle whether flows lead returns or if returns lead flows. For example, Hayley (2014) shows that IRRs may be pushed upwards by increasing inflows following bad performance and increasing outflows following good performance. SGAR only measures the relation between flows and subsequent returns. However, SGAR is rigid by construction and is only effective at measuring a relation between flows and subsequent returns if mispricing reverses in a month's time. Despite their strengths and weaknesses, the IRR and SGAR measures complement each other by providing two distinct means of evaluating investor performance.

Starting with our sample of mature ETFs, we restrict the analysis to 412 ETFs with at least 36 consecutive months of data. For each ETF, we calculate its realized IRR and SGAR and test the statistical significance of each measure via Monte Carlo simulation using 100,000 sample paths. To simulate each ETF's IRR distribution, we follow the methodology of Dichev (2007) and shuffle the vector of capital contributions (as a percentage of beginning-of-month assets) with replacement using the stationary bootstrap technique of Politis and Romano (1994).<sup>36</sup> To simulate each ETF's SGAR distribution, we shuffle the vector of share growth  $\mathbf{g}$  with replacement also using a stationary bootstrap in each Monte Carlo path.

Figure 3 and Table 7 report the percentages of ETFs that have realized IRRs and SGARs in the left-tails of their simulated distributions.<sup>37</sup> Figure 3 depicts histograms of realized p-values (i.e., the percentage of simulated returns below the realized return); in each plot, p-values appear on the horizontal axis and frequencies appear on the vertical axis. For reference, the density function for a uniform distribution is included as a horizontal line in each plot. If IRRs and SGARs were not

<sup>36</sup> The stationary bootstrapping is characterized by  $p = 1/5$ .

<sup>37</sup> In Internet Appendix Table IA20, we show the percentages of ETFs which have realized IRRs and SGARs in the right-tails of their simulated distributions.

skewed distributions, the realized p-values would resemble a uniform distribution. Instead, both IRRs and SGARs exhibit negative skew; the left-hand portion of realized frequencies is consistently above the uniform distribution and the right-hand portion of realized frequencies is consistently below the uniform distribution.

Table 7 analyses the entire sample of ETFs and then considers two sub-samples: 2007-2011 and 2012-2016. For each sample of data, we report the percentages of ETFs falling below 1%, 5%, and 10% of the observations in their simulated distribution. In the 2007-2016 sample, both the IRR and the SGAR exhibit negative skew. 1.96% of ETFs (8 of 412) have an IRR that is smaller than 1% of the simulated IRRs in their respective distributions and 3.16% of ETFs (13 of 412) have a SGAR that is smaller than 1% of the simulated SGARs in their respective distributions. To put these numbers in perspective, the probabilities of 8 and 13 observations (or more) falling below a 1% threshold with 412 draws from a uniform distribution are 5.77% and 0.03%.<sup>38</sup> The percentage of ETFs with IRRs in the 5% and 10% left-tails are 7.09% (by chance this would occur with probability 4.23%) and 14.18% (by chance this would occur with probability 0.52%). For SGARs, the percentages of ETFs in the 5% and 10% left-tails are 11.41% (by chance, <0.01%) and 17.96% (by chance, <0.01%).

In the 2007-2011 sample, the IRR skew is less pronounced as compared to the full sample. The percentage of ETF IRR p-values falling in the left-tail are 2.19% (by chance, 11.26%), 6.56% (by chance, 20.70%) and 13.11% (by chance, 10.30%) for the 1%, 5% and 10% thresholds respectively. The SGAR skew, however, is more pronounced in the 2007-2011 sample as compared to the full sample. The percentage of ETF SGAR p-values falling in the left-tail are 3.83% (by chance, 0.26%), 11.48% (by chance, 0.04%), and 22.40% (by chance, <0.01%) for the three threshold values respectively. The 2012-2016 sample exhibits greater IRR distribution skew and less SGAR distribution skew as compared to the full sample. The percentage of ETF IRR p-values falling in the left-tail are 4.43% (by chance, <0.01%), 14.29% (by chance, <0.01%), and 23.65% (by chance, <0.01%) and the percentage of ETF SGAR p-values falling in the left-tail are 0.74% (by chance, 77.20%), 7.14% (by chance, 3.61%), and 13.05% (by chance, 2.78%).

<sup>38</sup> The probabilities are computed under the assumption that each ETF's p-value is i.i.d. and drawn from a uniform distribution.

The results in Figure 3 and Table 7 show that realized ETF IRRs and SGARs tend to have a negative tilt relative to the expectation under the null hypothesis, implying that ETF investors underperform over time. The IRR analysis suggests that ETF investors collectively underperform the performance on a single share. As an anecdotal example, consider State Street Global Advisor's fund SPY which is the largest ETF in the world and represented \$226 billion in assets at the end of 2016. ETF investors' IRR in SPY underperformed the return on a single share by 37 bps per year. The SGAR analysis also suggests that ETF investors mistime their asset allocation decisions between risky and safe assets. SPY's SGAR of 5.43% differs from its simulated expected SGAR of 6.91% by 148 bps per year. Thus, while SPY's management fee is 9 bps annually, our IRR and SGAR analysis suggests that non-fundamental demand imposes indirect costs on investors that are an order of magnitude larger than the ETF's management fee.<sup>39</sup>

## 6. Conclusion

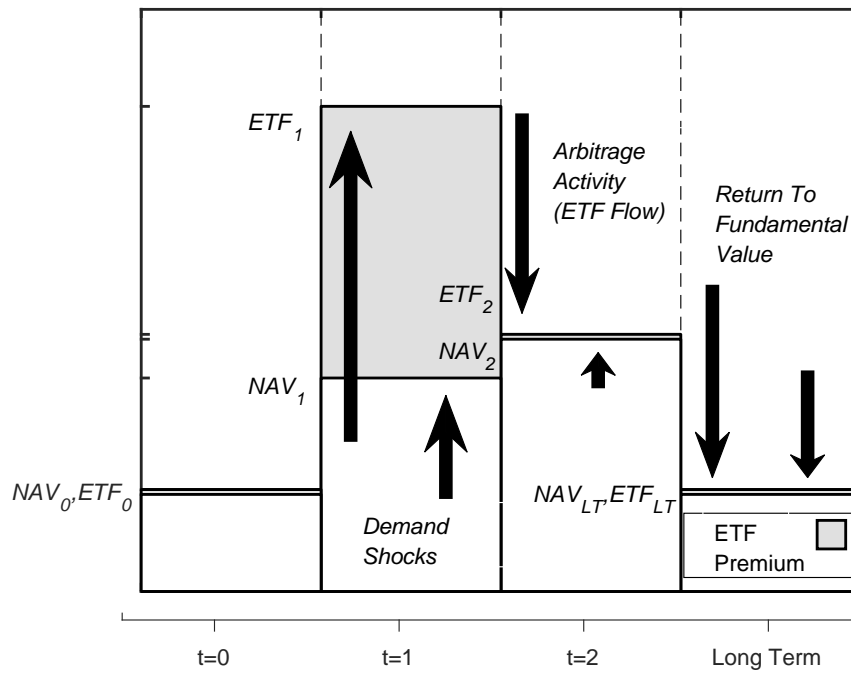
We show theoretically and empirically that ETF flows contain a strong signal of non-fundamental demand. ETFs with large inflows predictably earn lower future returns than ETFs with large outflows. Moreover, we find that non-fundamental demand causes ETF investors to systematically mistime their investments, leading to a reduction in their profits. Our findings suggest several areas of future research. By showing that non-fundamental demand shocks have different effects at the one-, three-, and six-month horizons, our results suggest there may be additional variation in non-fundamental demand that impacts asset prices at different horizons. Put differently, future research should investigate the term-structure of non-fundamental demand shocks and the speed at which they reverse. More generally, our analysis shows that ETFs are a novel laboratory for studying the impact of non-fundamental demand shocks.

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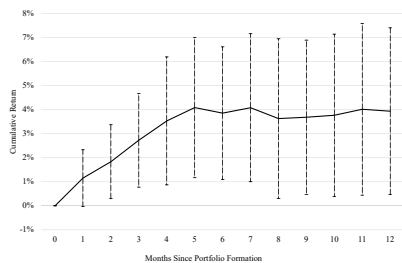
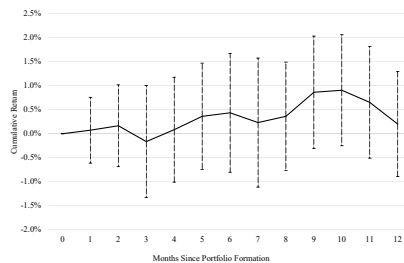
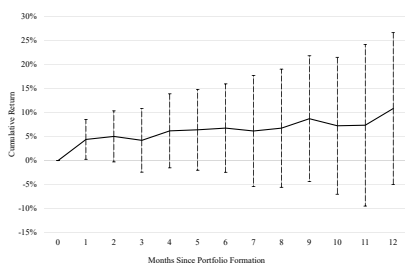
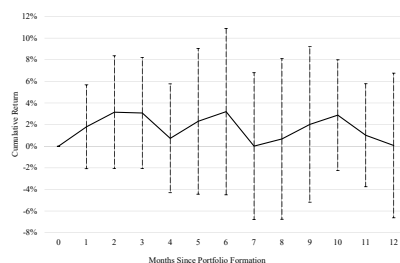
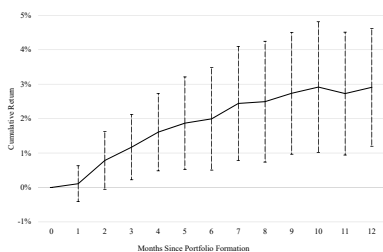
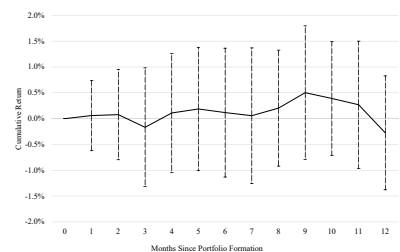
<sup>39</sup> Our results do not say that the ETF mechanism leads to underperformance. Rather, the ETF mechanism provides the means to measure the costs of non-fundamental demand.

*Fig. 1.* ETF Flows and ETF Premia Changes as Signals of Non-Fundamental Demand Shocks

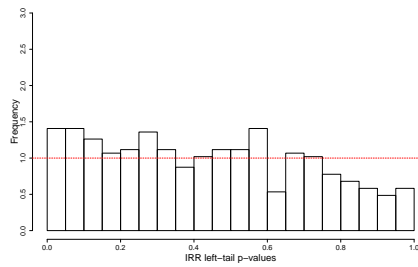
At  $t = 0$ , no mispricing exists between the ETF share price ( $ETF_0$ ) and the ETF net asset value ( $NAV_0$ ) and both are priced at their shared fundamental value. At  $t = 1$ , imbalanced non-fundamental demand shocks generate a mispricing by pushing the ETF share price and the ETF NAV away from their shared value. At  $t = 2$ , arbitrageurs restore relative price efficiency, putting upward price pressure on the ETF NAV and downward price pressure on the ETF share price. In the long term, the ETF and NAV prices revert back to their shared fundamental value.



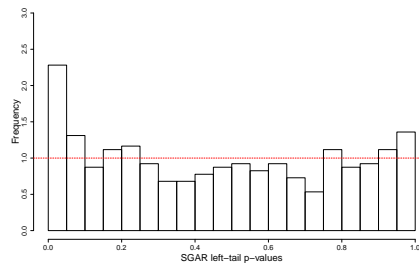
*Fig. 2.* Returns to Long-Short Portfolios Based on ETF Returns Each month, ETFs are sorted based on the prior month's *ETFFlow* or *ETFPremChange*. ETFs with the highest redemption activity or most negative premium change are sorted into Decile 1, while ETFs with the highest creation activity or most positive premium change are sorted into Decile 10. Value-weighted portfolio returns are calculated by forming long-short portfolios, which are long Decile 1 ETFs and short Decile 10 ETFs. Portfolio returns are calculated using ETF returns for the 12 months following formation, and each horizon's returns are averaged across months. Error bars provide the 95% confidence interval for each average return.

(a) Mature ETFs: *ETFFlow*(b) Mature ETFs: *ETFPremChange*(c) Lev. ETFs: *ETFFlow*(d) Lev. ETFs: *ETFPremChange*(e) Unlev. ETFs: *ETFFlow*(f) Unlev. ETFs: *ETFPremChange*

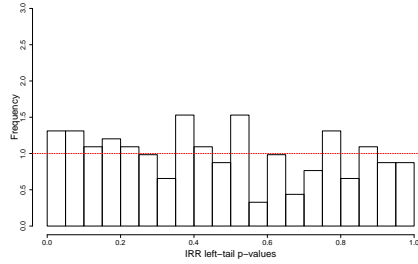
*Fig. 3.* Histogram of p-values for realized ETF IRRs and SGARs. Each histogram reports the p-values corresponding to realized internal rate of returns (IRRs) and share-growth-adjusted returns (SGARs) based on their simulated distributions. A uniform distribution's density function is depicted in each histogram for reference (dotted red line). The left column of histograms corresponds to IRRs and the right column corresponds to SGARs.



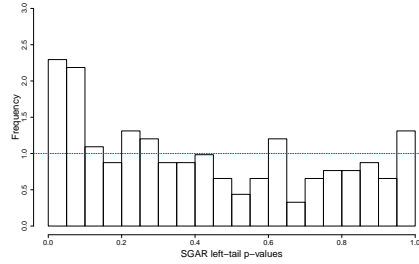
(a) IRR: 2007-2016



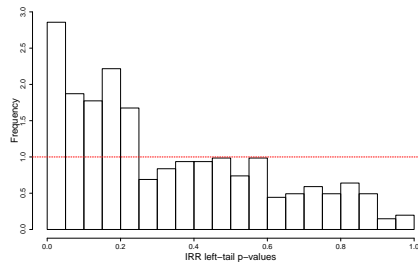
(b) SGAR: 2007-2016



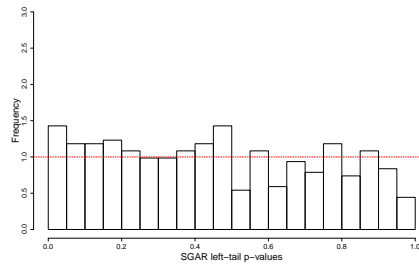
(c) IRR: 2007-2011



(d) SGAR: 2007-2011



(e) IRR: 2012-2016



(f) SGAR: 2012-2016

*Table 1* Yearly ETF Sample

ETFs are included in the \$50M+ sample from the first month in which end-of-month market capitalization exceeds \$50 million. \$50M+ ETFs are considered mature from the first month in which creation or redemption activity was reported on at least 50% of trading days. Leveraged ETFs include long (2X and 3X) and short (-1X, -2X and -3X) funds. We require at least twelve months of data for an ETF to be included in our sample. Number and Market capitalization are measured at the end of each calendar year. Market capitalization is reported in billions.

Year	All ETFs		\$50M+ ETFs		Mature ETFs		Mature Unleveraged		Mature Leveraged	
	Number	Market Cap	Number	Market Cap	Number	Market Cap	Number	Market Cap	Number	Market Cap
2007	559	\$605	370	\$603	124	\$516	119	\$511	5	\$5
2008	667	\$532	445	\$530	178	\$468	159	\$451	19	\$17
2009	769	\$774	524	\$769	226	\$687	189	\$662	37	\$25
2010	927	\$993	635	\$988	270	\$891	225	\$865	45	\$26
2011	1,119	\$1,044	731	\$1,039	331	\$956	278	\$929	53	\$26
2012	1,205	\$1,341	807	\$1,336	360	\$1,223	301	\$1,200	59	\$23
2013	1,299	\$1,682	910	\$1,677	408	\$1,529	344	\$1,501	64	\$28
2014	1,409	\$1,976	1029	\$1,971	439	\$1,785	370	\$1,757	69	\$28
2015	1,576	\$2,108	1113	\$2,103	516	\$1,914	436	\$1,885	80	\$29
2016	1,515	\$2,526	1101	\$2,513	518	\$2,275	438	\$2,246	80	\$29

Table 2 ETF Sample Characteristics

ETFs are included in the \$50M+ sample from the first month in which end-of-month market capitalization exceeds \$50 million. \$50M+ ETFs are considered mature from the first month in which creation or redemption activity was reported on at least 50% of trading days. Leveraged ETFs include long (2X and 3X) and short (-1X, -2X and -3X) funds. Trading days are considered active if the number of shares outstanding changed, indicating either creation or redemption activity. Average Creation/Redemption Activity is measured by aggregating the absolute value of daily percentage changes in shares outstanding at the monthly level. The Lipper category “Bonds” includes ETFs classified as “Mixed” or “Municipal,” and the “Commodities” category includes ETFs classified as “Currency.”

	All ETFs	\$50M+ ETFs	Mature ETFs	Mature Unleveraged	Mature Leveraged	High Activity Unleveraged
<b>Average ETF Characteristics</b>						
Shares Outstanding (millions)	20.9	30.0	60.0	68.3	13.3	111.1
Average Monthly Volume (millions)	24	35	76	71	107	165
Average Monthly Volume (% of shares out)	82%	94%	158%	79%	602%	149%
ETF Market Capitalization (billions)	\$1.2	\$1.7	\$3.5	\$4.0	\$0.5	\$7.6
Bid-Ask Spread	0.34%	0.19%	0.10%	0.10%	0.10%	0.06%
Short Interest Percentage	5.7%	6.7%	11.6%	11.9%	9.8%	25.6%
Average Premium	0.10%	0.09%	0.09%	0.11%	-0.01%	0.29%
Percentage of Active Days	15.9%	21.8%	36.9%	37.5%	34.0%	64.4%
Average Creation/Redemption Activity	14.4%	15.2%	19.5%	16.6%	35.8%	31.2%
Monthly Observations	126,668	87,710	38,283	32,545	5,738	10,792
<b>Lipper Category Percentages</b>						
Broad Equities	33.8%	33.6%	33.2%	25.7%	76.0%	32.7%
Sector Equities	23.0%	23.8%	28.6%	33.1%	2.9%	35.6%
Bonds	18.5%	17.7%	13.9%	14.1%	12.8%	16.5%
Commodities	5.2%	6.1%	6.9%	6.7%	8.4%	5.3%
International	18.7%	18.7%	17.4%	20.5%	0.0%	9.9%

Table 3 Portfolio Sorts on ETF Flow: ETF Returns

Each month, ETFs are sorted based on the prior month's *ETFFlow*. ETFs with the highest redemption activity are sorted into Decile 1, while ETFs with the highest creation activity are sorted into Decile 10. Raw ETF return differences are tested by forming long-short portfolios, which are long high redemption ETFs and short high creation ETFs. In Panel B, ETFs are first sorted based on the prior month's primary market activity, which is measured as the number of days with changes in shares outstanding. ETFs are then sorted based on the prior month's *ETFFlow*. \*\*\*, \*\*, \* indicate statistical significance at the 1%, 5%, and 10% levels using Newey-West standard errors with the lag equal to the return horizon in months.

<b>Panel A: Baseline Results</b>									
	One Month			Three Months			Six Months		
	Decile 1	Decile 10	Long-Short	Decile 1	Decile 10	Long-Short	Decile 1	Decile 10	Long-Short
<b>\$50M+ ETFs</b>									
Equal-Weighted	0.587*	-0.932**	1.519***	0.788	-1.546**	2.334***	1.423	-2.157**	3.580***
Value-Weighted	0.738*	-0.395	1.134**	1.684**	-0.979	2.663***	2.794**	-0.991	3.785***
<b>Mature ETFs</b>									
Equal-Weighted	0.704**	-1.321***	2.025***	0.695	-1.880**	2.575***	1.272	-2.519**	3.791***
Value-Weighted	0.689*	-0.465	1.154*	1.686**	-1.044	2.730***	2.951**	-0.908	3.859***
<b>Mature, Leveraged ETFs</b>									
Equal-Weighted	1.072	-3.380***	4.452***	-0.972	-5.015**	4.043	-2.639	-8.024***	5.385
Value-Weighted	1.310	-3.099**	4.409**	-0.820	-5.039**	4.219	-1.573	-8.343**	6.771
<b>Mature, Unleveraged ETFs</b>									
Equal-Weighted	0.238	0.063	0.175	0.959	0.523	0.435	2.183	1.009	1.175*
Value-Weighted	0.441	0.331	0.110	1.636**	0.466	1.170**	3.022**	1.028	1.994***
<b>Panel B: Mature, Unleveraged ETFs</b>									
	One Month			Three Months			Six Months		
	Decile 1	Decile 10	Long-Short	Decile 1	Decile 10	Long-Short	Decile 1	Decile 10	Long-Short
<b>Low Activity ETFs</b>									
Equal-Weighted	0.257	0.844*	-0.586**	1.122	1.917**	-0.795*	2.555*	3.205**	-0.651
Value-Weighted	0.378	0.880*	-0.502	1.441*	1.390	0.050	2.360*	2.663*	-0.303
<b>Medium Activity ETFs</b>									
Equal-Weighted	0.376	-0.007	0.383	0.892	0.421	0.470	1.734	1.001	0.733
Value-Weighted	0.257	0.423	-0.165	1.009	0.471	0.538	1.699	0.586	1.113
<b>High Activity ETFs</b>									
Equal-Weighted	0.388	-0.025	0.413	1.066	-0.156	1.222**	2.602**	0.091	2.512***
Value-Weighted	0.690	0.273	0.416	1.697**	0.157	1.539**	3.609***	0.277	3.332***

Table 4 Portfolio Sorts on ETF Flows: NAV Returns

Each month, ETFs are sorted based on the prior month's *ETFFlow*. ETFs with the highest redemption activity are sorted into Decile 1, while ETFs with the highest creation activity are sorted into Decile 10. Raw NAV return differences are tested by forming long-short portfolios, which are long high redemption ETFs and short high creation ETFs. In Panel B, ETFs are first sorted based on the prior month's primary market activity, which is measured as the number of days with changes in shares outstanding. ETFs are then sorted based on the prior month's *ETFFlow*. \*\*\*, \*\*, \* indicate statistical significance at the 1%, 5%, and 10% levels using Newey-West standard errors with the lag equal to the return horizon in months.

<b>Panel A: Baseline Results</b>									
	One Month			Three Months			Six Months		
	Decile 1	Decile 10	Long-Short	Decile 1	Decile 10	Long-Short	Decile 1	Decile 10	Long-Short
<b>\$50M+ ETFs</b>									
Equal-Weighted	0.537*	-0.906**	1.444***	0.664	-1.501**	2.165***	1.240	-2.128**	3.368***
Value-Weighted	0.718*	-0.411	1.129**	1.613**	-0.948	2.561***	2.695**	-0.976	3.671***
<b>Mature ETFs</b>									
Equal-Weighted	0.663**	-1.308***	1.971***	0.564	-1.838**	2.403***	1.075	-2.527**	3.602***
Value-Weighted	0.674	-0.479	1.153*	1.609**	-1.024	2.633***	2.847**	-0.913	3.760***
<b>Mature, Leveraged ETFs</b>									
Equal-Weighted	0.974	-3.330***	4.304**	-1.233	-5.004**	3.771	-2.957	-8.054***	5.097
Value-Weighted	1.315	-2.988**	4.303**	-0.912	-4.939**	4.027	-1.740	-8.258**	6.518
<b>Mature, Unleveraged ETFs</b>									
Equal-Weighted	0.200	0.081	0.120	0.875	0.596	0.279	2.058	1.070	0.988
Value-Weighted	0.415	0.305	0.110	1.590**	0.511	1.079**	2.953**	1.069	1.884**
<b>Panel B: Mature, Unleveraged ETFs</b>									
	One Month			Three Months			Six Months		
	Decile 1	Decile 10	Long-Short	Decile 1	Decile 10	Long-Short	Decile 1	Decile 10	Long-Short
<b>Low Activity</b>									
Equal-Weighted	0.199	0.823*	-0.625**	0.973	1.987**	-1.014**	2.384*	3.202**	-0.818
Value-Weighted	0.350	0.862*	-0.512	1.332	1.525	-0.192	2.295*	2.666*	-0.371
<b>Medium Activity</b>									
Equal-Weighted	0.339	0.039	0.300	0.802	0.507	0.296	1.610	1.047	0.563
Value-Weighted	0.230	0.460	-0.230	0.946	0.544	0.401	1.616	0.659	0.956
<b>High Activity</b>									
Equal-Weighted	0.352	0.013	0.339	1.007	-0.065	1.071**	2.500*	0.200	2.300***
Value-Weighted	0.639	0.279	0.360	1.648**	0.206	1.442**	3.528***	0.332	3.196***

Table 5 Panel Regressions of ETF Returns on ETF Flows

The table displays panel regressions of monthly ETF returns (in percent) on measures of past creation and redemption activity according to the model:

$$Performance_{j,t+h} = \beta FlowMeasure_{j,t} + \gamma_t + \delta V_{j,t} + \epsilon_{j,t+h},$$

in which  $Performance_{j,t+h}$  is a measure of ETF  $j$ 's performance (i.e., raw return including distributions,  $Ret$ , or abnormal returns using the Fama-French three-factor plus momentum (Carhart, 1997) factor returns,  $AbnRet$ ) at horizon  $h$ ,  $h$  is either one month, three months, or six months,  $FlowMeasure_{j,t}$  is either the set of indicator variables  $Decile_{j,d,t}$  for whether ETF  $j$  is in decile portfolio  $d$  in period  $t$  (from sorting on  $ETFFlow_{j,t}$ ) or the continuous measure  $ETFFlow_{j,t}$ ,  $\gamma_t$  are date fixed effects, and  $V_{j,t}$  are lagged fund controls of ETF return (two lags), ETF premium, ETF share volume and ETF market capitalization.  $ETFFlow$  and ETF characteristics are standardized by subtracting the sample mean and dividing by the sample standard deviation.  $t$ -statistics calculated using Driscoll-Kraay standard errors with the lag equal to the return horizon in months are shown below the estimates in parentheses. \*\*\*, \*\*, \* indicates statistical significance at the 1%, 5%, and 10% levels.

	One Month			Three Months			Six Months		
	(1) <i>Ret</i>	(2) <i>AbnRet</i>	(3) <i>AbnRet</i>	(4) <i>Ret</i>	(5) <i>AbnRet</i>	(6) <i>AbnRet</i>	(7) <i>Ret</i>	(8) <i>AbnRet</i>	(9) <i>AbnRet</i>
Decile2	-0.49* (-1.76)	-0.36** (-2.36)		0.09 (0.21)	-0.20 (-0.67)		0.80 (1.16)	-0.22 (-0.48)	
Decile3	-0.41 (-1.40)	-0.35** (-2.32)		0.42 (0.90)	-0.25 (-0.84)		1.05 (1.30)	-0.54 (-1.13)	
Decile4	-0.48 (-1.62)	-0.41*** (-2.70)		0.56 (1.06)	-0.20 (-0.71)		1.46 (1.56)	-0.45 (-0.98)	
Decile5	-0.30 (-0.95)	-0.21 (-1.19)		0.82 (1.39)	0.34 (1.12)		1.75* (1.77)	0.16 (0.29)	
Decile6	-0.27 (-0.83)	-0.29* (-1.89)		0.94 (1.62)	0.04 (0.13)		2.16** (2.29)	-0.24 (-0.46)	
Decile7	-0.23 (-0.82)	-0.22 (-1.44)		0.86 (1.57)	0.20 (0.75)		1.74* (1.82)	-0.04 (-0.07)	
Decile8	-0.39 (-1.34)	-0.22 (-1.50)		0.38 (0.72)	0.09 (0.31)		1.29 (1.42)	-0.14 (-0.27)	
Decile9	-0.67** (-2.27)	-0.36** (-2.10)		-0.28 (-0.48)	-0.06 (-0.17)		-0.05 (-0.05)	-0.20 (-0.30)	
Decile10	-1.86*** (-4.05)	-0.79*** (-4.28)		-2.10*** (-3.29)	-0.76** (-2.36)		-3.75*** (-4.75)	-1.58** (-2.55)	
<i>ETFArb</i>			-0.03 (-1.16)			-0.04 (-1.08)			-0.05 (-1.28)
Date Fixed Effects	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Lagged Controls	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
$R^2$	0.197	0.033	0.032	0.220	0.042	0.041	0.236	0.049	0.047
Observations	37,759	37,759	37,759	36,711	36,711	36,711	35,139	35,139	35,139

Table 6 Trading Strategy Performance

Each month, ETFs are sorted based on the prior month's *ETFFlow*. ETFs with the highest redemption activity are sorted into Decile 1, while ETFs with the highest creation activity are sorted into Decile 10. Portfolio returns are calculated by forming long-short value-weighted portfolios, which are long high redemption ETFs and short high creation ETFs. For one-month returns, the portfolios are only based on the prior month's *ETFFlow*, so the portfolio turns over every month. For six-month returns, the portfolio equally-weights each of the last six months' one-month portfolios, so one-sixth of the portfolio turns over every month. Returns, standard deviations, and Sharpe ratios are all annualized. Unleveraged high activity ETFs are unleveraged ETFs in the top tercile of creation/redemption activity each period. Panel A includes the full sample. Panel B analyzes portfolio returns that occurred from 2007-2011 and Panel C analyzes portfolio returns that occurred from 2012-2016. The 2012-2016 sample therefore uses data from the end of 2011 in forming the portfolios in early 2012.

Panel A: Full Sample	One Month			Six Months		
	Mature ETFs	Leveraged ETFs	Unleveraged High Activity ETFs	Mature ETFs	Leveraged ETFs	Unleveraged High Activity ETFs
	Mean Annual Return	11.96%	27.21%	3.07%	8.03%	8.08%
Standard Deviation	19.84%	74.42%	13.97%	8.08%	39.76%	7.42%
Sharpe Ratio	0.60	0.37	0.22	0.99	0.20	0.82
Maximum Monthly Loss	-14.52%	-54.98%	-8.21%	-7.80%	-47.91%	-6.34%

Panel B: 2007-2011	One Month			Six Months		
	Mature ETFs	Leveraged ETFs	Unleveraged High Activity ETFs	Mature ETFs	Leveraged ETFs	Unleveraged High Activity ETFs
	Mean Annual Return	19.86%	21.42%	9.12%	12.27%	-12.38%
Standard Deviation	26.63%	94.74%	17.78%	10.72%	52.39%	9.15%
Sharpe Ratio	0.75	0.23	0.51	1.14	-0.24	1.06
Maximum Monthly Loss	-14.52%	-50.41%	-8.21%	-7.80%	-47.91%	-6.34%

Panel C: 2012-2016	One Month			Six Months		
	Mature ETFs	Leveraged ETFs	Unleveraged High Activity ETFs	Mature ETFs	Leveraged ETFs	Unleveraged High Activity ETFs
	Mean Annual Return	4.66%	31.98%	-2.59%	3.99%	27.48%
Standard Deviation	8.39%	54.20%	8.28%	3.60%	26.08%	4.96%
Sharpe Ratio	0.55	0.59	-0.31	1.11	1.05	0.52
Maximum Monthly Loss	-7.20%	-54.98%	-7.82%	-2.61%	-24.35%	-4.06%

*Table 7* Distributions of Internal Rates of Return and Share-Growth-Adjusted Returns

The table presents realized internal rates of return (IRRs) and share-growth-adjusted returns (SGARs) compared to their simulated distributions. Three time period samples are analyzed: 2007-2016 (the full sample), 2007-2011, and 2012-2016. For each sample, the Table reports the percentage of ETFs falling in the left-tail of their simulated distributions at thresholds of 1%, 5%, and 10%. The first three columns correspond to IRRs and the second three columns correspond to SGARs.

	IRR			SGAR		
	1%	5%	10%	1%	5%	10%
Entire Sample Equal-Weighted <i>N</i> = 412	1.96%	7.09%	14.18%	3.16%	11.41%	17.96%
Jan. 2007-Dec. 2011 Equal-Weighted <i>N</i> = 183	2.19%	6.56%	13.11%	3.83%	11.48%	22.40%
Jan. 2012-Dec. 2016 Equal-Weighted <i>N</i> = 406	4.43%	14.29%	23.65%	0.74%	7.14%	13.05%

## Appendix

### Proof of Lemma 1:

Each authorized participant  $i$ 's optimization is given explicitly by,

$$\max_{\delta \in \mathfrak{R}} \delta_i \left( \left( \beta + \Omega_0 + \nu_2^{etf} - \eta (q_0 + \delta_i + \delta_{-i}) \right) - \left( \Omega_0 + \nu_2^{nav} + \lambda (\delta_i + \delta_{-i}) \right) \right), \quad (\text{A1})$$

in which  $\delta_{-i}$  is the total redemption/creation activity for all other  $N - 1$  authorized participants and,

$$\nu_2^{etf} = \omega_1 + \epsilon^{etf}, \quad (\text{A2})$$

$$\nu_2^{nav} = \omega_1 + \epsilon^{nav}, \quad (\text{A3})$$

since the authorized participants cannot disentangle the fundamental shock from the non-fundamental shocks. The optimization in Equation A1 simplifies to,

$$\max_{\delta \in \mathfrak{R}} \delta_i \left( \left( \nu_2^{etf} - \eta (\delta_i + \delta_{-i}) \right) - \left( \nu_2^{nav} + \lambda (\delta_i + \delta_{-i}) \right) \right), \quad (\text{A4})$$

and the first-order condition with respect to  $\delta_i$  yields,

$$0 = \left( \left( \nu_2^{etf} - \eta (\delta_i + \delta_{-i}) \right) - \left( \nu_2^{nav} + \lambda (\delta_i + \delta_{-i}) \right) \right) + \delta_i (-\eta - \lambda). \quad (\text{A5})$$

Solving for  $\delta_i$  gives,

$$\delta_i = \frac{\nu_2^{etf} - \nu_2^{nav} - \delta_{-i}(\lambda + \eta)}{2(\lambda + \eta)}. \quad (\text{A6})$$

All authorized participants face the same optimization problem and their equilibrium choice  $\delta^*$  is implicitly given by,

$$\delta^* = \frac{\nu_2^{etf} - \nu_2^{nav} - (N - 1)\delta^*(\lambda + \eta)}{2(\lambda + \eta)}, \quad (\text{A7})$$

and explicitly given by,

$$\delta^* = \frac{\nu_2^{etf} - \nu_2^{nav}}{(N + 1)(\lambda + \eta)} \quad (\text{A8})$$

$$= \frac{\epsilon^{etf} - \epsilon^{nav}}{(N+1)(\lambda + \eta)}. \quad (\text{A9})$$

Furthermore, the aggregate ETF flow is given by,

$$\Delta^* = N\delta^* \quad (\text{A10})$$

$$= \frac{N(\epsilon^{etf} - \epsilon^{nav})}{(N+1)(\lambda + \eta)}. \quad (\text{A11})$$

The limit of  $\Delta^*$  as  $N \rightarrow \infty$  is given by,

$$\lim_{N \rightarrow \infty} \Delta^* = \frac{\epsilon^{etf} - \epsilon^{nav}}{\lambda + \eta}. \quad (\text{A12})$$

### Proof of Lemma 2:

The proof follows immediately from taking the variance of  $\lim_{N \rightarrow \infty} \Delta^*$ .

### Proof of Proposition 1:

The equilibrium ETF share price is given by,

$$p^* = \beta + \Omega_2 - \eta(q_0 + \Delta^*) + \epsilon^{etf}, \quad (\text{A13})$$

which simplifies to,

$$p^* = \Omega_0 + \omega_1 + \epsilon^{etf} - \eta \left( \frac{N(\epsilon^{etf} - \epsilon^{nav})}{(N+1)(\lambda + \eta)} \right). \quad (\text{A14})$$

The equilibrium NAV price is given by,

$$\pi^* = \Omega_2 + \epsilon^{nav} + \lambda\Delta_1, \quad (\text{A15})$$

which simplifies to,

$$\pi^* = \Omega_0 + \omega_1 + \epsilon^{nav} + \lambda \left( \frac{N(\epsilon^{etf} - \epsilon^{nav})}{(N+1)(\lambda + \eta)} \right). \quad (\text{A16})$$

Using the equilibrium ETF share price and NAV price, the  $t = 2$  equilibrium ETF premium is given by,

$$* = \left( 1 - \frac{N}{N+1} \right) (\epsilon^{etf} - \epsilon^{nav}), \quad (\text{A17})$$

the  $t = 2$  equilibrium ETF fundamental mispricing is given by,

$$\varphi^* = \epsilon^{etf} - \eta \left( \frac{N(\epsilon^{etf} - \epsilon^{nav})}{(N+1)(\lambda + \eta)} \right), \quad (\text{A18})$$

and the  $t = 2$  equilibrium NAV fundamental mispricing is given by,

$$\alpha^* = \epsilon^{nav} + \lambda \left( \frac{N(\epsilon^{etf} - \epsilon^{nav})}{(N+1)(\lambda + \eta)} \right). \quad (\text{A19})$$

Taking the limits of  $\psi^*$ ,  $\varphi^*$ , and  $\alpha^*$  as  $N \rightarrow \infty$  yields,

$$\lim_{N \rightarrow \infty} \psi^* = 0, \quad (\text{A20})$$

$$\lim_{N \rightarrow \infty} \varphi^* = \epsilon^{etf} \frac{\lambda}{\lambda + \eta} + \epsilon^{nav} \frac{\eta}{\lambda + \eta}, \quad (\text{A21})$$

$$\lim_{N \rightarrow \infty} \alpha^* = \epsilon^{etf} \frac{\lambda}{\lambda + \eta} + \epsilon^{nav} \frac{\eta}{\lambda + \eta}. \quad (\text{A22})$$

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