

# Revisiting the relation between the number of globular clusters and galaxy mass for low-mass galaxies

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## ABSTRACT

Using a new method to estimate total galaxy mass ( $M_T$ ) and two samples of low-luminosity galaxies containing measurements of the number of globular clusters (GCs) per galaxy ( $N_{GC}$ ), we revisit the  $N_{GC}$ – $M_T$  relation using a total of 203 galaxies, 157 of which have  $M_T \leq 10^{10} M_\odot$ . We find that the relation is nearly linear,  $N_{GC} \propto M_T^{0.92 \pm 0.08}$  down to at least  $M_T \sim 10^{8.75} M_\odot$ . Because the relationship extends to galaxies that average less than one GC per galaxy and to a mass range in which mergers are relatively rare, the relationship cannot be solely an emergent property of hierarchical galaxy formation. The character of the radial GC distribution in low-mass galaxies, and the lack of mergers at these galaxy masses, also appears to challenge models in which the GCs form in central, dissipatively concentrated high-density, high-pressure regions and are then scattered to large radius. The slight difference between the fitted power-law exponent and a value of one leaves room for a shallow  $M_T$ -dependent variation in the mean mass per GC that would allow the relation between total mass in GCs and  $M_T$  to be linear.

**Key words:** globular clusters: general – galaxies: formation – galaxies: star clusters: general.

## 1 INTRODUCTION

One of the more intriguing relationships among galaxy properties is that between the number of globular clusters ( $N_{GC}$ ), or total mass contained therein ( $M_{GC}$ ), and total galaxy mass,  $M_T$  (Blakeslee, Tonry & Metzger 1997; Georgiev et al. 2010; Harris, Harris & Alessi 2013; Hudson, Harris & Harris 2014; Forbes et al. 2016; Harris, Blakeslee & Harris 2017; Forbes et al. 2018; Burkert & Forbes 2020). Such a relationship suggests that most GCs form primarily in ways disconnected to how galaxies form the bulk of their stars (cf., Spitler & Forbes 2009; Hudson et al. 2014), which in turn implies distinct star formation modes during galaxy evolution.

It is tempting to speculate that the  $N_{GC}$ – $M_T$  and  $M_{GC}$ – $M_T$  relations provide a critical clue to GC formation. However, generic models where GC formation occurs predominantly at high redshift, in progenitor dark matter haloes that are aggregated by hierarchical assembly into the galaxies we see today, can begin to reproduce the observed trend without resorting to exotic theories (Boylan-Kolchin 2017; Choksi & Gnedin 2019; El-Badry et al. 2019; Bastian et al. 2020; Burkert & Forbes 2020). In fact, El-Badry et al. (2019) demonstrated that even when GCs are assigned randomly to progenitor haloes, the galaxies eventually formed from those haloes satisfy the relations. The ‘fog’ of hierarchical assembly apparently obscures our view of GC formation.

However, those same studies demonstrated that this interpretation would be challenged if the relationships extend to low-mass galaxies, as some had already suggested to be the case (Hudson et al. 2014; Zaritsky, Crnojević & Sand 2016; Harris et al. 2017), where mergers are less common and galaxies do not build up primarily

through multiple hierarchical events (Fitts et al. 2018; Martin et al. 2021). Indeed, Forbes et al. (2018) extended the  $M_{GC}$ – $M_T$  relation to masses well below where the fiducial model prediction of El-Badry et al. (2019) deviates from linearity and Bastian et al. (2020) emphasised that they predict a turnover in the  $M_{GC}$ – $M_T$  relation. This is an important tension that merits further investigation, with implications for models of galaxy evolution and GC formation. As illustrated by Burkert & Forbes (2020) and Bastian et al. (2020), there is a compelling case for precisely determining the nature of the relationship between GCs and galaxy mass as far down the galaxy mass function as possible.

The principal obstacles we face in extending and refining the  $N_{GC}$  or  $M_{GC}$  versus  $M_T$  relations in low-mass galaxies are the small numbers of GCs per galaxy at these galaxy masses and the paucity of mass measurements for such galaxies. For example, the Forbes et al. (2018) sample includes only 22 galaxies with  $M_T < 10^{10} M_\odot$ , where  $10^{10} M_\odot$  is roughly the lower mass limit of previous studies (e.g. Spitler & Forbes 2009) and is one example of a hypothesized threshold mass below which galaxies do not form GCs (El-Badry et al. 2019). Fortunately, two recent studies (Forbes et al. 2020; Carlsten et al. 2022) provide measurements of  $N_{GC}$  for large samples of low luminosity galaxies. Unfortunately, there are yet no corresponding  $M_T$  measurements for these samples and it is difficult to measure internal kinematics for such a large number of faint, low surface brightness galaxies. This paucity of data results in state-of-the-art statistical studies focusing on the relation between  $N_{GC}$  or  $M_{GC}$  and  $M_*$  instead of  $M_T$  (e.g. Eadie, Harris & Springford 2022).

Faced with this challenge, we propose to obtain  $M_T$  estimates for these galaxies using a new method that relies on galaxy scaling relations and, after doing so, examine the low-mass behaviour of the  $N_{GC}$ – $M_T$  relation. Although our approach is manifestly less precise,

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and potentially less accurate, than evaluating  $M_T$  from spectroscopic kinematic measurements, the small numbers of GCs per galaxy ( $\lesssim 1$ ) for the lowest mass galaxies in these samples inherently limits the precision with which any galaxy can ever be placed on the  $N_{GC}-M_T$  relation. Therefore, precise  $M_T$  measurements offer little return on investment, given the high observational cost of measuring the internal kinematics of these galaxies. Rather than working with a few galaxies where one axis in this space is inherently imprecise, we propose working with many galaxies where both axes are imprecise and recovering precision through averaging. We focus on  $N_{GC}-M_T$  rather than  $M_{GC}-M_T$  to stay closer to the observations, particularly for these galaxies where the mean GC mass is not well established. In Section 2, we briefly describe the published literature data we are using. In Section 3, we present our approach to estimating  $M_T$  and supporting evidence for the accuracy of the approach on average. In Section 4, we discuss the results and summarize in Section 5. We adopt WMAP9 cosmological parameter (Hinshaw et al. 2013) and a solar  $V$ -band absolute magnitude of 4.81 (Willmer 2018).

## 2 THE DATA

We use two sources of  $N_{GC}$  measurements for low luminosity galaxies (Forbes et al. 2020; Carlsten et al. 2022). The Forbes et al. (2020) study examines the GC populations of low surface brightness galaxies in the Coma cluster, with a focus on ultra-diffuse galaxies (those with  $r_e > 1.5$  kpc). They compiled measurements of  $N_{GC}$  for 76 galaxies from other studies (van Dokkum et al. 2017; Lim et al. 2018; Amorisco et al. 2018) within the footprint of the Subaru imaging they use to measure galaxy properties (Alabi et al. 2020) and complement their galaxy structure measurements with an additional 9 from Lim et al. (2018). Here, we use only the 76 systems in common between Forbes et al. (2020) and Alabi et al. (2020) to ensure homogeneity among the structural parameters we utilize in the scaling relations used to derive galaxy masses.

The details of the completeness corrections used to correct both for those GCs that are below the detection limit and for those that lie beyond the adopted search radius are critical when comparing  $N_{GC}$  measurements among studies. At the distance of the Coma cluster, the corrections can often be greater than a factor of 2 (e.g. van Dokkum et al. 2016) and highly uncertain. Saifollahi et al. (2022) use deep *HST* imaging to derive more precise constraints on the GC luminosity function and radial distribution for six Coma cluster ultra-diffuse galaxies. They find a luminosity function that is consistent with what was previously assumed and in agreement with that for GCs in other dwarf galaxies, but a radial distribution that is consistent with that of the stars and is thus different than that typically assumed, resulting in significantly revised, smaller completeness corrections. To reconcile the  $N_{GC}$  values compiled by Forbes et al. (2020) to these newer findings, we use the five galaxies in common between the Forbes et al. (2020) and Saifollahi et al. (2022) samples, to derive a median multiplicative correction of 0.27 for the Forbes et al. (2020)  $N_{GC}$  values. However, we caution that because the Forbes et al. (2020) sample is itself a compilation of  $N_{GC}$  values from different studies, a single recalibration may be insufficient. Unfortunately, we do not have enough overlap with each of the different studies incorporated to correct each independently.

If nothing else, this attempted recalibration illustrates the degree to which completeness corrections can affect the overall normalization of  $N_{GC}$ . It is the largest source of uncertainty in the comparison among studies or to theoretical models. For further reference, had we chosen to correct by the mean rather than the median ratio then the ‘corrected’  $N_{GC}$  values would be nearly two-thirds larger than

what we are actually adopting. An error in this correction will affect an entire sample similarly and, therefore, will not affect conclusions regarding the linearity of the  $N_{GC}-M_T$  relation within the sample. However, it will result in offsets among studies, which is why having results from at least two different ones provides a valuable check.

The second study we use is that of Carlsten et al. (2022), which presents  $N_{GC}$ , complemented by Carlsten et al. (2021) for the other necessary parameters for 145 low luminosity early-type galaxies in the Local Volume. The imaging data are sufficiently deep that they reach below the peak of the GC luminosity function. The GC radial distribution is extensively examined and discussed. For both of these reasons, and the fact that we have no overlapping measurements, we do not apply any multiplicative correction to their  $N_{GC}$  measurements. Because of the larger size and the homogeneity of the  $N_{GC}$  measurements, this is our preferred sample, but as we will show our results from the two samples are consistent.

In both samples, there are some galaxies with  $N_{GC} \leq 0$  due to statistical background subtraction. The uncertainties at the smallest values of  $N_{GC}$  are dominated by the large background correction rather than the Poisson statistics of  $N_{GC}$  and therefore still closer to Gaussian in nature. These uncertainties are also significantly larger than those introduced by the completeness corrections (magnitude limit and radial distribution) if the GC populations of the low-mass systems are not dramatically different than those of brighter systems where these corrections have been calibrated. As such, we do not anticipate a measurement bias near  $N_{GC} = 0$  towards positive values of  $N_{GC}$ .

## 3 ESTIMATING TOTAL MASS

In a series of papers (Zaritsky, Gonzalez & Zabludoff 2006a,b; Zaritsky, Zabludoff & Gonzalez 2008, 2011), we presented an extension of the Fundamental Plane formalism (Djorgovski & Davis 1987; Dressler et al. 1987) that applies to the entire family of galaxies. Particularly relevant to the current discussion, the revised scaling relation applies to low-mass stellar systems (Zaritsky et al. 2006b, 2011) and to ultra-diffuse galaxies (Zaritsky 2017). In the last of those studies, we exploited the relationship between the half-light radius,  $r_e$ , the surface brightness within  $r_e$ ,  $I_e$ , and a measure of the internal kinematics,  $V$ , to estimate  $V$ , from which we then recovered the mass-to-light ratio within  $r_e$ ,  $\Upsilon_e$ , and hence the mass within that same radius. Specifically, there are two equations that are empirically calibrated:

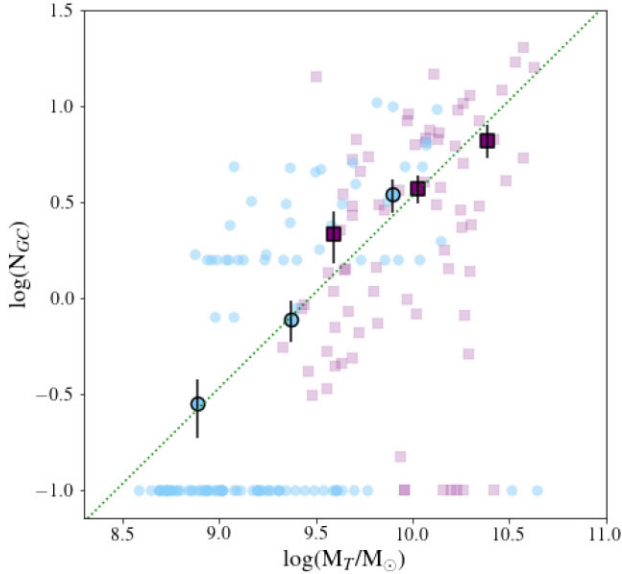
$$\log r_e = 2 \log V - \log I_e - \log \Upsilon_e - 0.8, \quad (1)$$

$$\log \Upsilon_e = 0.24 (\log V)^2 + 0.12 (\log I_e)^2 - 0.32 \log V - 0.83 \log I_e - 0.02 \log V I_e + A, \quad (2)$$

where the coefficients in equation (2) were obtained by fitting to a large sample of galaxies (Zaritsky 2012). We specifically call out the constant  $A$  and discuss it further below. The kinematic term,  $V$ , is defined to be the combination of the line-of-sight velocity dispersion,  $\sigma_v$ , and the inclination corrected rotation speed,  $v_r$ ,  $V \equiv \sqrt{\sigma_v^2 + v_r^2}/2$ . These two equations can be rewritten as one and numerically solved for  $V$  when one is given  $r_e$  and  $I_e$ . In this specific version of the equations,  $r_e$  is in units of kpc,  $I_e$  in  $M_\odot \text{pc}^{-2}$ ,  $V$  in  $\text{km s}^{-1}$ , and  $\Upsilon_e$  in solar units.

The constant  $A$  was also previously determined using measured values of  $r_e$ ,  $V$ , and  $I_e$  for the same large sample of galaxies. However, we adjust  $A$  slightly here to provide better agreement between our calculated values of  $M_T$  and those available from Forbes et al. (2018). We set  $A = 1.57$ , as opposed to the previous value of 1.49, and





**Figure 3.**  $N_{GC}$  versus  $M_T$  for the Forbes et al. (2020) sample (squares) and Carlsten et al. (2022) sample (circles). Lightly coloured symbols without error bars are the results for individual galaxies in either sample, while the darker symbols with error bars represent means and the dispersion in the means. Individual systems with  $N_{GC} \leq 0$  are plotted at  $\log(N_{GC}) = -1$ , but the actual values are used in the calculation of the means and their uncertainties. The dotted line represents the best-fitting power-law relation to the binned data.

is a necessary condition for the unbiased evaluation of the means and our use of the scatter about the mean to determine the uncertainty in the mean.

There are various results of note in the figure. First, the averages for the Forbes et al. (2020) and Carlsten et al. (2022) samples agree well. This result supports our recalibration of the Forbes et al. (2020)  $N_{GC}$  values, although we still caution against a detailed comparison between the two samples. Specifically, the agreement could be somewhat fortuitous and should not (yet) be used as evidence against environmental differences in the  $N_{GC}-M_T$  relation (Carlsten et al. 2022). Secondly, both sets of data together make a compelling case for the near linearity of the  $N_{GC}-M_T$  relation to as small a mass as available in the samples,  $M_T \sim 10^8 M_\odot$ . When we allow for a non-linear power law,  $N_{GC} = A M_T^\beta$ , our best fit to the binned data,  $\beta = 0.92 \pm 0.08$ , is statistically consistent with a linear relation. We conclude that we find no evidence for a deviation from a linear relation down to masses of  $\sim 10^{8.75} M_\odot$ . Thirdly, at these limiting low masses, each galaxy has on average  $\sim 0.3$  GC’s, which illustrates how difficult it will be to extend the relationship to even lower masses. Fourthly, our best-fitting linear relation for all of the binned data is for one GC per  $(2.9 \pm 0.3) \times 10^9 M_\odot$ . This result calls for a larger number of GCs per unit mass than determined previously (e.g. one GC per  $5 \times 10^9 M_\odot$ ; Burkert & Forbes 2020), but the offset is sufficiently modest ( $< 2$ ) that it could be due to either systematics in the GC completeness corrections or in the definition of  $M_T$ . The dominant uncertainties in our fitted normalization are not included in the quoted formal uncertainty. As one example, the choice we made to adjust the value of  $A$  in equation (2) affects the overall normalization of the relationship and the agreement between the Forbes et al. (2020) and Carlsten et al. (2022), although the latter is also at the mercy of our recalibration of the Forbes et al. (2020)  $N_{GC}$  values. Fortunately, those uncertainties do not qualitatively affect any of our other key findings.

The precision of the fitted power-law exponent poses a number of challenges to models of globular cluster formation and evolution:

1. First, it unequivocally confirms the findings of Forbes et al. (2018) that the relation between the nature of the GC population and  $M_T$  extends at least 2.5 orders of magnitude in mass below where the El-Badry et al. (2019) fiducial model relationship turns over and about 1.5 orders of magnitude in mass below the adopted limiting mass for haloes that host GC formation. As noted by El-Badry et al. (2019), the fiducial model has various parameters that can be altered and at least the limiting halo mass could be decreased somewhat relative to the fiducial model (e.g., Valenzuela et al. 2021). However, the  $N_{GC}-M_T$  relation now clearly extends well below the mass range where mergers dominate galaxy growth (Fitts et al. 2018; Martin et al. 2021), which argues against the hypothesis that the relationship is simply an emergent property of hierarchical galaxy formation.

2. Secondly, it establishes to high precision that this relation is indeed nearly linear, despite what is expected to be a complicated interplay of GC formation and destruction phenomena present in most models (e.g. Ashman & Zepf 1992; Elmegreen & Efremov 1997; Kravtsov & Gnedin 2005; Kruijssen 2015; Bastian et al. 2020). For massive galaxies, the model ‘details’ are thought to be mostly obscured through the homogenizing effects of hierarchical growth (Boylan-Kolchin 2017). Indeed, El-Badry et al. (2019) demonstrated that even a model with a random allocation of GCs to haloes at early times would produce the observed relationship for galaxies built up over time from other galaxies. However, the lower mass systems included here may typically experience only a single merger (Martin et al. 2021), if even that, and modifications in GC formation model ‘details’ should have results that are far more evident in the galaxies explored here.

3. Thirdly, it emphasizes the importance of the relation in terms of numbers of GCs. Most studies have focused on the  $M_{GC}-M_T$  relation, partly because  $M_{GC}$  is dominated by the more massive GCs, which are less susceptible to tidal destruction and evaporation. However, the near linearity of the  $N_{GC}-M_T$  relation reaffirms it as another useful mass proxy even for low mass galaxies. If we assume that the  $M_{GC}-M_T$  relation is the one that is perfectly linear, then we infer that the mean GC mass  $\propto M_T^{0.08}$ , which in turn implies a  $\sim 30$  per cent decline in the mean GC mass going from galaxies with  $\log(M_T)$  of 10.5–9. This is at least qualitatively consistent with the trend measured by Jordán et al. (2006) for a different sample of galaxies. As such, we cannot yet conclude whether  $N_{GC}$  or  $M_{GC}$  is more directly tied to  $M_T$ .

4. Fourthly, it confirms GC formation as a consistent, common phenomenon across many orders in galaxy mass, even within galaxies that on average host fewer than one GC. This finding is somewhat surprising given that we expect low-mass galaxies will have difficulties cooling gas and generating the extreme conditions envisioned in GC formation and evolution. Indeed, this is along the lines of the argument put forward by El-Badry et al. (2019) for a threshold halo mass in their model. GC formation models tend to posit the creation of high-pressure, high-density gas discs at large redshifts (Elmegreen & Efremov 1997; Kravtsov & Gnedin 2005; Kruijssen 2015) in which GCs form and may be tidally destroyed before mergers scatter the GCs into the galaxy halo (Kruijssen 2015). This process would have to have a nearly constant efficiency across at least 4 orders of halo mass to reproduce the observed relationships (7 orders of magnitude if these results can be grafted on to those discussed by Burkert & Forbes (2020)). Furthermore, any scenario that involves redistribution of GCs by mergers faces a related challenge in that the GC distributions in these low mass systems are not disc like and closely resemble the underlying stellar



distributions in both their radial and azimuthal distributions (Carlsten et al. 2022; Saifollahi et al. 2022).

From a different perspective, the near linearity of the  $N_{GC}-M_T$  relation supports the use of the galaxy scaling relations for determining  $M_T$ . While  $N_{GC}$  has been used as a mass proxy (e.g. van Dokkum et al. 2016; Amorisco et al. 2018; Forbes et al. 2020), measuring  $N_{GC}$  is also observationally challenging. The use of the scaling relation methodology will open up far larger samples for study.

A contrasting opinion is presented by Bastian et al. (2020) who emphasize that the masses assigned to these low-luminosity galaxies in GC studies are in conflict with those derived from the stellar mass–halo mass relation,  $M_*-M_T$ . They favour using the halo masses estimated from  $M_*-M_T$ , which do reproduce the downturn in the  $M_{GC}-M_T$  relation produced by their simulations. Thus, there is a clear tension between dynamically estimated masses (such as those estimated here and by Forbes et al. 2020) for low-mass galaxies and those estimated using  $M_*-M_T$ . The fault is not attributed to the determination of the mass within  $r_e$  but rather in the extrapolation to  $M_T$ . The discrepancies can be larger than an order of magnitude (Bastian et al. 2020), which seem to us difficult to reconcile with our rather direct use of NFW profiles to estimate  $M_T$ . In further support of our determination of  $M_T$  we note that a systematic error in  $M_T$  estimation would be unlikely to result in the observed precisely linear  $N_{GC}-M_T$  relation. For example, replacing our estimates of  $M_T$  with those derived from the Moster, Naab & White (2018)  $M_*-M_T$  relation using the parameters they derive for all galaxies at  $z = 0.1$  results in  $\beta = 1.83 \pm 0.36$ , which is a  $2.3\sigma$  deviation from linearity. As such, the tension remains and is an interesting avenue for further investigation.

## 5 SUMMARY

Using a new method with which to estimate the total mass of galaxies and two existing large sample of galaxies with measurements of the number of globular clusters (Forbes et al. 2020; Carlsten et al. 2022), we revisit the relationship between the number of globular clusters (GCs) a galaxy hosts,  $N_{GC}$ , and its total mass,  $M_T$ . We confirm previous findings (Forbes et al. 2018) that the relation extends to low  $M_T$ ,  $\sim 10^{8.75} M_\odot$ , and use these larger samples to place tight constraints on the power-law nature of the relationship,  $N_{GC} \propto M_T^{0.92 \pm 0.08}$ . For an adopted linear relation, we find one GC per  $(2.9 \pm 0.3) \times 10^9 M_\odot$  of total galaxy mass, although this number has significant additional uncertainty beyond the formal quoted uncertainty that is related to the adopted GC completeness corrections and estimation of  $M_T$ .

The nearly linear behaviour of the relationship places strong constraints on models, particularly since this behaviour extends to galaxy masses well below where galaxies have less than one GC on average. Any potential threshold halo mass for the production of GCs lies below  $10^{8.75} M_\odot$ , and the correlation between  $N_{GC}$  and  $M_T$ , at least at the lowest masses, cannot be an emergent property of the hierarchical growth of galaxies. Models that invoke mergers and interactions as a means either to trigger cluster formation or to redistribute clusters into the galaxy haloes (e.g. Kruijssen 2015) will also face challenges because the  $N_{GC}-M_T$  relation extends to masses where mergers are uncommon (Fitts et al. 2018; Martin et al. 2021).

We believe that these results motivate the investigation of novel GC formation models, such as the one proposed based on streaming motions of baryons in the early universe (Naoz & Narayan 2014; Schauer et al. 2021). Extending the  $N_{GC}-M_T$  relation to even lower

masses is a challenge, but there are indications that even ultrafaint galaxies can host GCs (Crnojević et al. 2016) and that on average these galaxies continue the  $N_{GC}-M_T$  relation to even lower masses (Zaritsky et al. 2016). GCs have played an oversized role in our understanding of the Universe, ranging from helping us to uncover the nature of our own galaxy (Shapley 1918) and others (Hubble 1932) to developing a theory of the evolution of stars and stellar populations (Sandage & Schwarzschild 1952). They may yet reveal additional fundamental astrophysics.

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## DATA AVAILABILITY

No new data were generated or analysed in support of this research.

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